Study of Wind Turbine based SEIG under Balanced/Unbalanced Loads and Excitation

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ABSTRACT
This paper presents the performance of a stand-alone self-excited induction generator (SEIG) driven by fixed pitch wind turbine. The main objective of the paper is: (i) dynamic study of SEIG under balanced R-L/R-C loads (ii) dynamic study of SEIG under balanced and unbalanced excitation, (iii) Fixed pitch wind turbine model has been considered for driving induction generator. An approach based on dynamic equations of an isolated SEIG under balanced/un-balanced conditions of loads is employed to study the behaviour of the system. The SEIG model with balanced/un-balanced load and excitation has been simulated using MATLAB/SIMULINK.

Keywords: Self excited induction generator, Wind turbine, R-L and R-C loads, Balanced/unbalanced excitation, Balanced/unbalanced loads

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1. INTRODUCTION
Renewable energy integration in the existing power systems is the demand in future due to the environmental concerns with conventional power plants. There is emphasis on the generation of power from the renewable sources. In this context, induction generator is becoming popular for power generation with non-conventional energy sources [1]. Self excitation process in induction generators makes the machine for applications in isolated power systems [2]. Various models have been proposed for steady state and transient analysis of self excited induction generator (SEIG) [3-17]. The d-q reference frame model, impedance based model, admittance based model, operational circuit based model, and power equations based models are frequently used for analysis of SEIG [3-17]. The overview of self excited induction generator issues has been provided in [19]. The transient/dynamic analysis of SEIG is reported in [10, 20-22]. The literature has also been reported by many researchers on wind driven self excited induction generator in [24-30]. State space model of self excited induction generator has been presented in [31-33]. A. Kishore et al. [32] proposed a generalized state-space dynamic modeling of a three phase SEIG developed using d-q variables in stationary reference frame for transient analysis.

The state space approach has been proposed for representation of transient operation of SEIG. The d-q axes stator-rotor current are the functions of machine parameters. The solution of such equation has been obtained assuming all the non linear parameters. The modelling of excitation system under balanced/un-balanced conditions has been developed in terms of d-q reference. Different constraints such as variation of excitation, wind speed and load have been taken into account and accordingly the effect on generated voltage and current has been analyzed. The effect of excitation capacitance on generated voltage has been analyzed [33]. Performance of wind turbine based SEIG with resistive load and balanced and unbalanced excitation was presented in [34].
In this paper work, an attempt has been made for an analysis of fixed pitch based SEIG and its dynamic behavior has been analyzed under R-L inductive load with balanced and unbalanced excitation conditions. The residual magnetism in the machine is taken into account in simulation process as it is necessarily required for the generator to self excite. Initial voltage in the capacitor is considered as 2 volts for build-up of voltage for excitation of SEIG. The simulations have been carried out developing model in MATLAB/SIMULINK [35]. The paper has been organized in different sections: section III describes SEIG mathematical model, section IV describes SIMULINK model of SEIG with load. In section V, results have been obtained for two cases of excitation under balanced and unbalanced condition with balanced inductive load.

2. SEIG MATHEMATICAL MODEL

The d-q axes equivalent circuit of a (SEIG) supplying an inductive load is shown in Fig. 1. A classical matrix formulation using d-q axes model is used to represent the dynamics of conventional induction machine operating as a generator and is given in (14). Using this matrix representation, we can obtain the instantaneous voltages and currents during the self-excitation process, as well as during load variations.

![Image](image1.png)

Figure 1. d-q axes equivalent circuit of SEIG

The complete dynamic model is represented by the set of eight differential equations corresponding to variables \(i_{ds}, i_{qs}, i_{dr}, i_{qr}, V_{ds}, V_{qs}\) as shown in equation (18) is the generalized state space representation of a SEIG model. That is in the form of classical state-space equation.

The dynamic model of the three-phase squirrel cage induction generator is developed by using stationary d-q axes reference frame and the relevant volt-ampere equations are as described as [12]:

\[
[V] = [R][i] + [L]p[i] + w[G][i]
\]

From which, the current derivative can be expressed as:

\[
p[i] = [L]^{-1} \{ [V] - [R][i] - w[G][i] \}
\]

\[
p[i] = - [L]^{-1} \{ [R][i] + w[G][i] - [V] \}
\]

where \([V],[i],[R],[L]\) and \([G]\) defined below:

\[
[V] = [V_{ds} V_{qs} V_{dr} V_{qr}]^T, [i] = [i_{ds} i_{qs} i_{dr} i_{qr}]^T, [R] = \text{diag}[R_s R_s R_r R_r],
\]

\[
L = \begin{bmatrix}
L_s & 0 & L_m & 0 \\
0 & L_s & 0 & L_m \\
L_m & 0 & L_r & 0 \\
0 & L_m & 0 & L_r
\end{bmatrix}
\]
2.1. Load and Capacitor Modeling

Load: Here the modeling of load has been developed in terms of d-q reference frame under balanced conditions. The load currents in terms of their respective voltages have been discussed below:

\[ i_{ld} = \frac{1}{L}(V_{ld} - (R/L)i_{ld}), i_{lq} = \frac{1}{L}(V_{lq} - (R/L)i_{lq}) \]  

(3)

Balanced R-C load:

\[ I_{ld} = C_L \rho (V_{ds} - R_{id}), I_{lq} = C_L \rho (V_{ds} - R_{i_0}) \]  

(4)

Figure 2 and 3 show the SIMLINK model of the balanced loads.

2.1.2. Capacitor model:

The capacitor has been modeled using equations (5), (6), (7) and (8) that represent the self excitation capacitor currents and voltages in d-q axes representation as [34]:

\[ i_{ds} = i_{cd} + i_{ld} \]  

(5)
\[ i_{qs} = i_{eq} + i_{q} \]  

(6)

\[
pV = \left( \frac{3}{2K_1} \right) \left( \frac{1}{C_1} + \frac{1}{C_2} \right) i_{u} + \left( \frac{3}{2K_2} \right) \left( \frac{1}{C_1} - \frac{1}{C_2} \right) i_{q}
\]

(7)

\[
pV = \left( \frac{3}{K_1} \right) \left( \frac{1}{K_2} \right) \left( \frac{1}{C_1} + \frac{1}{C_2} \right) \left[ i_{u} + \left( \frac{3}{K_1} \right) \left( \frac{1}{K_2} \right) \left( \frac{1}{C_1} - \frac{1}{C_2} \right) i_{q} \right]
\]

(8)

where

\[ K_1 = C_a + \left( \frac{C_b}{2} \right), \]

\[ K_2 = C_a + \left( \frac{C_c}{2} \right) \]

and \[ K_3 = \left( \frac{K_1}{C_a} \right) + \left( \frac{K_2}{C_c} \right) \]

If \[ C_a = C_b = C_c = C \] then it’s called as balanced self-excitation otherwise it’s called as un-balanced excitation. The SIMULINK model of excitation capacitor is shown in Fig. 4. This model describes the capacitor model for both balanced and unbalanced excitation conditions.

![Figure 4. Simulink Model of Capacitor](image)

The following assumptions have been considered are made in this analysis:

[i] Core and mechanical losses in the machine are neglected.

[ii] All machine parameters, except the magnetizing inductance \( L_m \), are assumed to be constant.

[iii] The rotor should have sufficient residual magnetism.

[iv] The three capacitor banks should be of sufficient value

[v] Stator voltage in terms of d-q, \( V_{ds} \) and \( V_{qs} \) should have some initial voltage i.e 1 volts.

The SEIG operates in the saturation region and its magnetizing characteristics are non-linear in nature. Magnetizing current is calculated in every step of integration in terms of stator and rotor d-q currents as:

\[ i_m = \sqrt{ \left( i_{d} + i_{q} \right)^2 + \left( i_{ds} + i_{qs} \right)^2 } \]  

(9)

Magnetizing inductance is calculated from the magnetizing characteristics which can be obtained by synchronous speed test for the machine under test. These characteristics can be defined as:

\[ L_m = 0.1407 + 0.0014i_m - 0.0012i_m^2 + 0.00005i_m^3 \]  

(10)

Developed electromagnetic torque of the SEIG is:

\[ T_e = \left( 3p_{pole}/4 \right) L_m (i_{ds}/i_{d} - i_{ds}/i_{q}) \]  

(11)
Torque balance equation is:

\[ T_{\text{shaft}} = T_e + j(2/p) \rho \omega_r \]  \hspace{1cm} (12)

The derivative of the rotor speed is:

\[ \rho \omega_r = (p/2) \left( T_{\text{shaft}} - T_e \right)/j \]  \hspace{1cm} (13)

The SIMULINK model of electromagnetic torque is given as:

![SIMULINK model of electromagnetic torque](image)

Figure 5. Electromagnetic torque

Using all subsystems developed in MATLAB, the complete model of SEIG with inductive and capacitive load and excitation is shown in Fig. 8 and is described in equation (14).

\[
\begin{bmatrix}
    i_p \\
    i_q \\
    \rho \\
    V_d \\
    V_q \\
    i_d \\
    i_q
\end{bmatrix} =
\begin{bmatrix}
    L R_i & -\omega L_i & -L R & -\omega L & L & 0 & 0 & 0 \\
    \omega L_i & L R & \omega L & -L R & 0 & L & 0 & 0 \\
    -L R & \omega L & L R & \omega L & -L & 0 & 0 & 0 \\
    -\omega L & L R & -L R & -\omega L & L R & 0 & -L & 0 \\
    0 & 0 & 0 & 0 & 0 & \frac{1}{\rho K} & \frac{1}{K} & 0 \\
    0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{K} & \frac{1}{K} \\
    0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{K}
\end{bmatrix}
\begin{bmatrix}
    i_p \\
    i_q \\
    \rho \\
    V_d \\
    V_q \\
    i_d \\
    i_q
\end{bmatrix} + 
\begin{bmatrix}
    V_m \\
    V_d \\
    V_q \\
    0 \\
    0 \\
    0 \\
    0
\end{bmatrix}
\]

(14)

where

\[
P = \begin{bmatrix}
    \frac{3}{2K} & \frac{1}{C} & \frac{1}{C}
\end{bmatrix},
Q = \begin{bmatrix}
    \sqrt{3} & \frac{1}{2K} & \frac{1}{C}
\end{bmatrix}
\]

(15)
\[
R = \left[ \frac{1}{C_1} \left( \frac{1}{K} + 1 \right) \right]^{-1} S = \left[ \frac{1}{C_1} \left( \frac{1}{K} + 1 \right) \right]^{-1}
\]

\[K = \frac{1}{L_m^2 - L_s L_r} \]

2.2. Wind Turbine Model

Fixed pitch wind turbine has been modeled to drive induction generator. The number of blades are taken as 3, blade radius equal is considered as 13m, and the gear ratio is taken as 30 with fixed pitch as \( \beta = 0 \). Since the power coefficient characteristic of wind turbine is a non-linear curve that reflects the aerodynamic behavior a wind turbine. The characteristic forms the basis for the custom turbine model. The non-linear, dimensionless \( C_p \) characteristic is represented as [32].

\[
C_p(\lambda, \beta) = C_1 \left( \frac{C_2}{\lambda_i} - C_3 \beta - C_4 \right) e^{-\frac{C_5}{\lambda_i}} + C_6 \lambda \]

\[\frac{1}{\lambda_i} = \frac{1}{\lambda + 0.08\beta} - \frac{0.035}{\beta^3 + 1}\]

where,

\[C_1 = 0.5176, \quad C_2 = 116, \quad C_3 = 0.4, \quad C_4 = 5, \quad C_5 = 21, \quad C_6 = 0.0068\]

The power coefficient function given by (20),

\[
P_m = 0.5 \rho A \left( \frac{116}{\lambda} - 9.06 e^{\frac{-21+0.735}{\lambda}} + 0.0068\lambda \right) v_w^3
\]

The mechanical torque is given as:

\[
t_m = 0.5 \rho A \left( \frac{116}{\lambda} - 9.06 e^{\frac{-21+0.735}{\lambda}} + 0.0068\lambda \right) v_w^3 \frac{R}{G v_w^2}
\]

The SIMULINK model of wind turbine is shown in Fig. 6. The \( C_p \) curve is obtained developing the wind turbine model in SIMULINK. The mechanical power output at air density of 1.1kpa is obtained as shown in Fig. 7.

![Figure 6. Custom wind turbine model (Air Density: 1.1 kpa)](image)
Using the dynamic equations described in the previous section, complete model of wind driven induction generator has been developed using MATLAB/SIMULINK toolbox [34]. The equations of self-excited induction generator for a data of 7.5 kW, 4 poles, $R_s=1\Omega$, $R_r=0.77\Omega$, $X_{lr}=X_{ls}=1\text{mH}$, $J=0.23\text{Kg/m}^2$ described above have been implemented in MATLAB/SIMULINK. The equation (14) has been implemented in subsystem “Induction Generator” whose outputs are currents. The complete MATLAB SIMULINK model is shown in Fig. 7 with subsystems components shown in color. Equation (14) shows the eight first order differential equations, for which the solutions gives the four currents (stator d-q axis currents and rotor d-q axis currents), load currents and capacitor voltages. Further these currents are the function of constants viz. stator and rotor inductances, resistances, speed, excitation capacitance and load impedance. The variables like magnetizing inductance, magnetizing currents, and electromagnetic torque generated, has been evaluated.

3. RESULTS AND ANALYSIS

In this paper, the results have been determined for SEIG with R-L loads taken under balanced conditions with balanced and unbalanced excitation. Two different cases taken for the study are:

Case 1: balanced R-L load and balanced excitation
Case 2: balanced R-L load and un-balanced excitation
Case 3: un-balanced R-L load and balanced excitation
Case 4: balanced R-C load and balanced excitation
Case 5: balanced R-C load and constant un-balanced excitation

These cases have been considered to observe the operation of SEIG and to analyze and the results for stator voltage, stator currents, load currents, and capacitor currents for all the cases.

3.1. SEIG Operation with R-L load

The operation of the SEIG is simulated with R=180 Ω, L=20 mH under balanced conditions and R_a = 180 Ω, R_b = 60 Ω, L_a = 20 mH, L_b = 0.001 mH, under unbalanced conditions. Generator is excited with C=110 µf and unbalanced excitation with C_a=110 µf, C_b=80 µf, C_c=103 µf. The results obtained with inductive R-L and R-C loads with balanced and unbalanced excitation are shown in Fig. 8 to 13.

3.1.1. Case-1: R-L balanced load and constant excitation:

In Case 1: balanced excitation with balanced inductive load, all the currents, i.e. stator currents, capacitor currents and load currents are balanced. Voltage is also balanced as shown in Fig. 6. It is observed from the Fig. 8 (graphs 1, 2, 3, 4) that the stator voltage, currents, load currents, and capacitor currents attain their steady state value at 4.5 sec. The variation of electromagnetic torque with time and magnetizing inductance with time of SEIG has also been shown in Fig. 8 (graphs 5 and 6). The electromagnetic torque is zero initially and then it increases exponentially and attains steady values at about 5.0 sec. It is observed that the magnetizing inductance is constant of value 0.14 H up to 3.5 sec. and then reduces to 0.103 H and become constant at 5.0 sec. and remains constant.
3.1.2. Case-2: Balanced R-L load and constant unbalanced excitation:

In Case 2: unbalanced excitation and balanced inductive load, the load currents are balanced but stator currents and capacitor currents are unbalanced as shown in Fig.9. It is observed from the Fig. 9 (graphs 1, 2, 3, 4) that the stator voltage, currents, load currents, and capacitor currents attain their steady state value at 4.5 sec. The variation of electromagnetic torque with time and magnetizing inductance with time of SEIG has also been shown in Fig. 9 (graphs 5 and 6). The electromagnetic torque is zero initially and then it increases exponentially and it is observed that Te is having oscillations due to unbalanced excitation. It is observed that the magnetizing inductance is constant of value 0.14 H up to 3.5 sec. and then reduces to 0.087 H and become constant at 5.0 sec. and remains constant.

Figure 8. SEIG at balanced Inductive (RL) load with constant excitation (graphs: 1. Stator line voltages 2. Stator currents 3. Load currents 4. Capacitor currents. 5. Electromagnetic torque. 6. Magnetizing inductance)
3.1.3. Case-3: Unbalanced RL load and balanced excitation

In Case 3: unbalanced inductive load and balanced excitation, all currents, stator currents, load currents are unbalanced but stator voltage and capacitor currents are balanced as shown in Fig. 10. It is observed from the Fig. 10 (graphs 1, 2, 3, 4) that the stator voltage, currents, load currents, and capacitor currents attain their steady state value at 3 sec. The variation of electromagnetic torque with time and magnetizing inductance with time of SEIG has also been shown in Fig. 10 (graphs 5 and 6). The electromagnetic torque is zero initially and then it increases exponentially and attains steady values at about 2.6 sec. Oscillations are observed for Te due to unbalanced load. It is observed that the magnetizing inductance is constant of value 0.14 H up to 3.6 sec. and then reduces to 0.085 H and small oscillations are observed due to the unbalanced load.
3.1.4. Case-4: Balanced RC load and balanced excitation

The operation of the SEIG is simulated with $R=160 \Omega$, $C=20 \, \mu F$ under balanced conditions. Generator is excited with $C=110 \, \mu F$ and unexcited with $C_a=110 \, \mu F$, $C_b=80 \, \mu F$, $C_c=103 \, \mu F$.

In Case4: balanced excitation with balanced RC-load all the currents, i.e. stator currents, capacitor currents and load currents are balanced. Voltage is also balanced as shown in Fig.11. It is observed from the Fig. 11 (graphs 1, 2, 3, 4) that the stator voltage, currents, load currents, and capacitor currents attain their steady state value at 4.2 sec. The variation of electromagnetic torque with time and magnetizing inductance with time of SEIG has also been shown in Fig. 11 (graphs 5 and 6). The electromagnetic torque is zero initially and then it increases exponentially and attains steady values at about 4.5 sec. It is observed that the magnetizing inductance is constant of value $0.14 \, H$ up to 3.5 sec. and then reduces to $0.085 \, H$ and become constant at 5.0 sec. and remains constant.
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3.1.5. Case-5: RC balanced load with constant un-balanced excitation

In Case 5: unbalanced excitation and balanced RC load, the load currents are balanced but stator currents and capacitor currents are un-balanced as shown in Fig.12. It is observed from the Fig.12 (graphs 1, 2, 3, 4) that the stator voltage, currents, load currents, and capacitor currents attain their steady state value late compared to Case 1 at 5.2 sec. The unbalanced excitation causes slow buildup of the voltage and currents. The variation of electromagnetic torque with time and magnetizing inductance with time of SEIG has also been shown in Fig.12 (graphs 5 and 6). The electromagnetic torque is zero initially and then it increases exponentially and it is observed that Te is having oscillations due to unbalanced excitation. It is observed that the magnetizing inductance is constant of value 0.14 H up to 4.5 sec. and then reduces to 0.095 H and become constant at 6 sec. and remains constant.
4. CONCLUSION

In this paper, the results have been determined for SEIG with R-L and R-C load under balanced and unbalanced excitation conditions. Based on the results for all the cases, the following conclusions can be drawn:

[i] The performance of SEIG has been determined for five different cases. It is observed that the performance of SEIG under balanced R-L and R-C and balanced excitations, the stator voltage, stator currents, load currents and capacitor currents are balanced. In this case the voltage build up is quite fast because of balanced excitation.

[ii] Under un-balanced excitation the electromagnetic torque is having oscillations compared to the case with balanced excitation and capacitor currents are unbalanced.

[iii] Under un-balanced load and balanced excitation the electromagnetic torque have more oscillations and are more as compared to other case.

[iv] It is observed that the stator currents and load currents are un-balanced under un-balanced load. It is balanced under balanced excitation and balanced load only.
REFERENCES


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