Advanced Active Power Filter Performance for Grid Integrated Hybrid Renewable Power Generation Systems

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ABSTRACT

An active power filter implemented with a four leg voltage-source inverter using a predictive control scheme is presented. The use of a four leg voltage-source inverter allows the compensation of current harmonic components, as well as unbalanced current generated by single-phase nonlinear loads. A detailed yet simple mathematical model of the active power filter, including the effect of the equivalent power system impedance, is derived and used to design the predictive control algorithm. The compensation performance of the proposed active power filter and the associated control scheme under steady state and transient operating conditions is demonstrated through simulations and experimental results.

Keywords:
Active power filter
Current control
Four-leg converters
Predictive control
Matlab/simulink

1. INTRODUCTION

Renewable generation affects power quality due to its nonlinearity, since solar generation plants and wind power generators must be connected to the grid through high-power static PWM converters [1]. The non uniform nature of power generation directly affects voltage regulation and creates voltage distortion in power systems. This new scenario in power distribution systems will require more sophisticated compensation techniques. Although active power filters implemented with three-phase four-leg voltage-source inverters (4L-VSI) have already been presented in the technical literature [2]-[6], the primary contribution of this paper is a predictive control algorithm designed and implemented specifically for this application. Traditionally, active power filters have been controlled using pre-tuned controllers, such as PI-type or adaptive, for the current as well as for the dc-voltage loops [7],[8]. PI controllers must be designed based on the equivalent linear model, while predictive controllers use the nonlinear model, which is closer to real operating conditions. An accurate model obtained using predictive controllers improves the performance of the active power filter, especially during transient operating conditions, because it can quickly follow the current-reference signal while maintaining a constant dc-voltage.

So far, implementations of predictive control in power converters have been used mainly in induction motor drives [9]-[16]. In the case of motor drive applications, predictive control represents a very intuitive control scheme that handles multivariable characteristics, simplifies the treatment of dead-time compensations, and permits pulse-width modulator replacement. However, these kinds of applications present disadvantages related to oscillations and instability created from unknown load parameters [17]-[26]. One advantage of the proposed algorithm is that it fits well in active power filter applications, since the power converter output parameters are well known [26]-[30]. These output parameters are obtained from the
converter output ripple filter and the power system equivalent impedance. The converter output ripple filter is part of the active power filter design and the power system impedance is obtained from well-known standard procedures [18]-[35]. In the case of unknown system impedance parameters, an estimation method can be used to derive accurate $R-L$ equivalent impedance model of the system [31]-[40]. This paper presents the mathematical model of the 4L-VSI and the principles of operation of the proposed predictive control scheme, including the design procedure [40]-[58]. The complete description of the selected current reference generator implemented in the active power filter is also presented. Finally, the proposed active power filter and the effectiveness of the associated control scheme compensation are demonstrated through simulation and validated with experimental results obtained in a 2 kVA laboratory prototype.

2. FOUR-LEG CONVERTER MODEL

Figure 1 shows the configuration of a typical power distribution system with renewable power generation. It consists of various types of power generation units and different types of loads. Renewable sources, such as wind and sunlight, are typically used to generate electricity for residential users and small industries. Both types of power generation use ac/ac and dc/ac static PWM converters for voltage conversion and battery banks for long term energy storage. These converters perform maximum power point tracking to extract the maximum energy possible from wind and sun. The electrical energy consumption behaviour is random and unpredictable, and therefore, it may be single or three-phase, balanced or unbalanced, and linear or nonlinear. An active power filter is connected in parallel at the point of common coupling to compensate current harmonics, current unbalance, and reactive power. It is composed by an electrolytic capacitor, a four-leg PWM converter, and a first-order output ripple filter, as shown in Figure 2. This circuit considers the power system equivalent impedance $Z_s$, the converter output ripple filter impedance $Z_f$, and the load impedance $Z_L$. The four-leg PWM converter topology is shown in Figure 3.

Figure 1. Stand-alone Hybrid Power Generation System with a Shunt Active Power Filter
This converter topology is similar to the conventional three-phase converter with the fourth leg connected to the neutral bus of the system. The fourth leg increases switching states from $8 (2^3$) to $16 (2^4$), improving control flexibility and output voltage quality [21]-[32], and is suitable for current unbalanced compensation. The voltage in any leg $x$ of the converter, measured from the neutral point ($n$), can be expressed in terms of switching states, as follows

$$v_{xn} = S_x - S_n v_{dc} \quad x = u, v, w, n$$  \hspace{1cm} (1)

The mathematical model of the filter derived from the equivalent circuit shown in Figure 2 is

$$V_0 = v_{xn} - R_{eq} i_0 - L_{eq} \frac{di_0}{dt}$$  \hspace{1cm} (2)

where $R_{eq}$ and $L_{eq}$ are the 4L-VSI output parameters expressed as Thevenin impedances at the converter output terminals $Z_{eq}$. Therefore, the Thevenin equivalent impedance is determined by a series connection of the ripple filter impedance $Z_f$ and a parallel arrangement between the system equivalent impedance $Z_s$ and the load impedance $Z_L$

$$Z_{eq} = \frac{Z_s Z_L}{Z_s + Z_f} + Z_f \quad Z_s + Z_f$$  \hspace{1cm} (3)
For this model, it is assumed that $Z_L \geq Z_s$, that the resistive part of the system’s equivalent impedance is neglected, and that the series reactance is in the range of 3–7% p.u., which is an acceptable approximation of the real system. Finally, in (2) $R_{eq} = R_f$ and $L_{eq} = L_s + L_f$.

3. DIGITAL PREDICTIVE CURRENT CONTROL

The block diagram of the proposed digital predictive current control scheme is shown in Figure 4. This control scheme is basically an optimization algorithm and, therefore, it has to be implemented in a microprocessor. Consequently, the analysis has to be developed using discrete mathematics in order to consider additional restrictions such as time delays and approximations [10], [22]–[27]. The main characteristic of predictive control is the use of the system model to predict the future behaviour of the variables to be controlled. The controller uses this information to select the optimum switching state that will be applied to the power converter, according to predefined optimization criteria. The predictive control algorithm is easy to implement and to understand, and it can be implemented with three main blocks as shown in Figure 4.

![Figure 4. Proposed Predictive Digital Current Control Block Diagram](image)

1) Current Reference Generator: This unit is designed to generate the required current reference that is used to compensate the undesirable load current components. In this case, the system voltages, the load currents, and the dc-voltage converter are measured, while the neutral output current and neutral load current are generated directly from these signals (IV).

2) Prediction Model: The converter model is used to predict the output converter current. Since the controller operates in discrete time, both the controller and the system model must be represented in a discrete time domain [22]. The discrete time model consists of a recursive matrix equation that represents this prediction system. This means that for a given sampling time $T_s$, knowing the converter switching states and control variables at instant $kT_s$, it is possible to predict the next states at any instant $(k + 1)T_s$. Due to the first-order nature of the state equations that describe the model in (1)–(2), a sufficiently accurate first-order approximation of the derivative is considered in this paper.

$$\frac{dx}{dt} = \frac{x[k+1] - x[k]}{T_s}$$

(4)

The 16 possible output current predicted values can be obtained from (2) and (4) as

$$i_0[k + 1] = \frac{T_s}{L_{eq}} (v_{sn}[k] - v_0[k]) + \left(1 - \frac{R_{eq}T_s}{L_{eq}}\right)i_0[k]$$

(5)
As shown in (5), in order to predict the output current $i_0$ at the instant $(k+1)$, the input voltage value $v_0$ and the converter output voltage $v_{xN}$, are required. The algorithm calculates all 16 values associated with the possible combinations that the state variables can achieve.

3) Cost Function Optimization: In order to select the optimal switching state that must be applied to the power converter, the 16 predicted values obtained for $i_0[k+1]$ are compared with the reference using a cost function $g$, as follows:

$$g[k+1] = (i_{on}[k+1] - i_{on}(k+1))^2 + (i_{on}[k+1] - i_{on}(k+1))^2 +$$

$$+ (i_{on}[k+1] - i_{on}(k+1))^2 + (i_{on}[k+1] - i_{on}(k+1))^2.$$  

(6)

The output current $i_0$ is equal to the reference ($i_0^r$) when $g = 0$. Therefore, the optimization goal of the cost function is to achieve a $g$ value close to zero. The voltage vector $v_{xN}$ that minimizes the cost function is chosen and then applied at the next sampling state. During each sampling state, the switching state that generates the minimum value of $g$ is selected from the 16 possible function values. The algorithm selects the switching state that produces this minimal value and applies it to the converter during the $k+1$ state.

4. CURRENT REFERENCE GENERATION

A $dq$-based current reference generator scheme is used to obtain the active power filter current reference signals. This scheme presents a fast and accurate signal tracking capability. This characteristic avoids voltage fluctuations that deteriorate the current reference signal affecting compensation performance [28]. The current reference signals are obtained from the corresponding load currents as shown in Figure 5.

![Figure 5. dq-based Current Reference Generator Block Diagram](image)

This module calculates the reference signal currents required by the converter to compensate reactive power, current harmonic and current imbalance. The displacement power factor ($\sin \phi (L)$) and the maximum total harmonic distortion of the load (THD $(_L)$) defines the relationships between the apparent power required by the active power filter, with respect to the load, as shown

$$\frac{S_{APF}}{S_L} = \sqrt{\frac{\sin \Phi (L) + THD (L)^2}{\sqrt{1 + THD (L)^2}}}$$

(7)
where the value of THD \( i_{dc} \) includes the maximum compensable harmonic current, defined as double the sampling frequency \( f_s \). The frequency of the maximum current harmonic component that can be compensated is equal to one half of the converter switching frequency.

The dq-based scheme operates in a rotating reference frame; therefore, the measured currents must be multiplied by the \( \sin(\omega t) \) and \( \cos(\omega t) \) signals. By using dq-transformation, the d current component is synchronized with the corresponding phase-to-neutral system voltage, and the q current component is phase-shifted by 90°. The \( \sin(\omega t) \) and \( \cos(\omega t) \) synchronized reference signals are obtained from a synchronous reference frame (SRF) PLL [29]. The SRF-PLL generates a pure sinusoidal waveform even when the system voltage is severely distorted. Tracking errors are eliminated, since SRF-PLLs are designed to avoid phase voltage unbalancing, harmonics (i.e., less than 5% and 3% in fifth and seventh, respectively), and offset caused by the nonlinear load conditions and measurement errors [30]. Equation (8) shows the relationship between the real currents \( i_{dq} (t) \) (\( x = u, v, w \)) and the associated dq components \( i_d \) and \( i_q \).

\[
\begin{bmatrix}
    i_d \\
    i_q
\end{bmatrix} = \frac{2}{\sqrt{3}}
\begin{bmatrix}
    \sin\omega t & \cos\omega t \\
    -\cos\omega t & \sin\omega t
\end{bmatrix}
\begin{bmatrix}
    \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\
    -\frac{\sqrt{3}}{2} & \frac{\sqrt{3}}{2} & \frac{\sqrt{3}}{2}
\end{bmatrix}
\begin{bmatrix}
    i_{Lu} \\
    i_{Lv} \\
    i_{Lw}
\end{bmatrix}
\]

(8)

A low-pass filter (LFP) extracts the dc component of the phase currents \( i_d \) to generate the harmonic reference components \( i_q \). The reactive reference components of the phase-currents are obtained by phase-shifting the corresponding ac and dc components of \( i_q \) by 180°. In order to keep the dc-voltage constant, the amplitude of the converter reference current must be modified by adding an active power reference signal \( i_{dc} \) with the d-component, as will be explained in Section IV-A. The resulting signals \( i'_d \) and \( i'_q \) are transformed back to a three phase system by applying the inverse Park and Clark transformation, as shown in (9). The cut off frequency of the LPF used in this paper is 20 Hz.

\[
\begin{bmatrix}
    i'_d \\
    i'_q \\
    i'_w
\end{bmatrix} = \frac{2}{\sqrt{3}}
\begin{bmatrix}
    \frac{1}{\sqrt{2}} & 1 & 0 \\
    1 & \frac{1}{2} & \frac{\sqrt{3}}{2} \\
    \frac{1}{\sqrt{2}} & 1 & \frac{\sqrt{3}}{2}
\end{bmatrix}
\begin{bmatrix}
    1 & 0 & 0 \\
    \sin\omega t & -\cos\omega t & 0 \\
    \cos\omega t & \sin\omega t & 0
\end{bmatrix}
\begin{bmatrix}
    i_d \\
    i_q \\
    i_w
\end{bmatrix}
\]

(9)

The current that flows through the neutral of the load is compensated by injecting the same instantaneous value obtained from the phase-currents, phase-shifted by 180°, as shown next

\[
i'_{on} = -(i_{Lu} + i_{Lv} + i_{Lw})
\]

(10)

One of the major advantages of the dq-based current reference generator scheme is that it allows the implementation of a linear controller in the dc-voltage control loop. However, one important disadvantage of the dq-based current reference frame algorithm used to generate the current reference is that a second order harmonic component is generated in \( i_d \) and \( i_q \) under unbalanced operating conditions. The amplitude of this harmonic depends on the percent of unbalanced load current (expressed as the relationship between the negative sequence current \( i_{L1,2} \) and the positive sequence current \( i_{L+} \)). The second-order harmonic cannot be removed from \( i_d \) and \( i_q \), and therefore generates a third harmonic in the reference current when it is converted back to abc frame [31]. Figure 6 shows the percent of system current imbalance and the percent of third harmonic system current, in function of the percent of load current imbalance. Since the load current does not have a third harmonic, the one generated by the active power filter flows to the power system.
4.1. DC-Voltage Control

The dc-voltage converter is controlled with a traditional PI controller. This is an important issue in the evaluation, since the cost function (6) is designed using only current references, in order to avoid the use of weighting factors. Generally, these weighting factors are obtained experimentally, and they are not well defined when different operating conditions are required. Additionally, the slow dynamic response of the voltage across the electrolytic capacitor does not affect the current transient response. For this reason, the PI controller represents a simple and effective alternative for the dc-voltage control. The dc-voltage remains constant (with a minimum value of $\sqrt{6} v_s$) until the active power absorbed by the converter decreases to a level where it is unable to compensate for its losses.

The active power absorbed by the converter is controlled by adjusting the amplitude of the active power reference signal $i_{es}$, which is in phase with each phase voltage. In the block diagram shown in Figure 5, the dc-voltage $v_{dc}$ is measured and then compared with a constant reference value $v_{dc}^*$. The error $e$ is processed by a PI controller, with two gains, $K_p$ and $T_i$. Both gains are calculated according to the dynamic response requirement. Figure 7 shows that the output of the PI controller is fed to the dc-voltage transfer function $G_s$, which is represented by a first-order system (11)

$$G(s) = \frac{v_{dc}}{i_e} = \frac{3 K_p v_s \sqrt{2}}{2 C_{dc} v_{dc}^*} \tag{11}$$

The equivalent closed-loop transfer function of the given system with a PI controller (12) is shown in (13)

$$C(s) = K_p (1 + \frac{1}{T_i s}) \tag{12}$$

$$\frac{v_{dc}}{i_e} = \frac{\omega_n^2 (s + a)}{s^2 + 2\delta \omega_n s + \omega_n^2} \tag{13}$$

Since the time response of the dc voltage control loop does not need to be fast, a damping factor $\zeta = 1$ and a natural angular speed $\omega_n = 2\pi \cdot 100 \text{ rad/s}$ are used to obtain a critically damped response with minimal voltage oscillation. The corresponding integral time $T_i = 1/a$ (13) and proportional gain $K_p$ can be calculated as
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\[
\delta = - \sqrt{3 \frac{K_p v_s \sqrt{2T_i}}{8 C_{dc} v_{dc}^2}}
\]

(14)

\[
\omega_n = - \sqrt{3 \frac{K_p v_s \sqrt{2}}{2 C_{dc} v_{dc} T_i}}
\]

(15)

Figure 7. DC-Voltage Control Block Diagram

5. SIMULATION RESULTS

A simulation model for the three-phase four-leg PWM converter with the parameters shown in Table I has been developed using MATLAB-Simulink. The objective is to verify the current harmonic compensation effectiveness of the proposed control scheme under different operating conditions. A six-pulse rectifier was used as a nonlinear load. The proposed predictive control algorithm was programmed using an S-function block that allows simulation of a discrete model that can be easily implemented in a real-time interface (RTI) on the dSPACE DS1103 R&D control board. Simulations were performed considering a 20 [\mu s] of sample time. In the simulated results shown in Figure 8, the active filter starts to compensate at \( t = t_1 \). At this time, the active power filter injects an output current \( i_{ou} \) to compensate current harmonic components, current unbalanced, and neutral current simultaneously. During compensation, the system currents \( i_\text{s} \) show sinusoidal waveform, with low total harmonic distortion (THD = 3.93\%). At \( t = t_2 \), a three-phase balanced load step change is generated from 0.6 to 1.0 p.u. The compensated system currents remain sinusoidal despite the change in the load current magnitude. Finally, at \( t = t_3 \), a single-phase load step change is introduced in phase \( u \) from 1.0 to 1.3 p.u., which is equivalent to an 11% current imbalance. As expected on the load side, a neutral current flow through the neutral conductor \( (i_{n,u}) \), but on the source side, no neutral current is observed \( (i_{n,a}) \). Simulated results show that the proposed control scheme effectively eliminates unbalanced currents. Additionally, Figure 8 shows that the dc-voltage remains stable throughout the whole active power filter operation.
6. EXPERIMENTAL RESULTS

The compensation effectiveness of the active power filter is corroborated in a 2 kVA experimental setup. A six-pulse rectifier was selected as a nonlinear load in order to verify the effectiveness of the current harmonic compensation. A step load change was applied to evaluate the transient response of the dc voltage loop. Finally, an unbalanced load was used to validate the performance of the neutral current compensation. Because the experimental implementation was performed on a dSPACE I/O board, all I/O Simulink blocks used in the simulations are 100% compatible with the dSPACE system capabilities. The complete control loop is executed by the controller every 20 $\mu$s, while the selected switching state is available at 16 $\mu$s. An average switching frequency of 4.64 kHz is obtained.

Figure 9 shows the transient response of the compensation scheme. Figure 9(a) shows that the line current becomes sinusoidal when the active power filter starts compensation, and the dc-voltage behaves as expected. (b) Voltage and system waveforms, $v_u$ and $i_u$, $i_{m}$, $i_{on}$. Consequence good tracking characteristic of the current references, as shown in Figure 9(d). In Figure 10, the transient response of the active power filter under a step load change is shown. The line currents remain sinusoidal and the dc-voltage returns to its reference with a typical transient response of an under damped second-order system (maximum overshoot of 5% and two cycles of settling time). In this case, a step load change is applied from 0.6 to 1.0 p.u. Finally, the load connected to phase u was increased from 1.0 to 1.3 p.u. The corresponding waveforms are shown in Figure 11. Figure 11(a) shows that the active filter is able to compensate the current in the neutral conductor with fast transient response. Moreover, Figure 11(b) shows that the system neutral current $i_{on}$ is effectively compensated and eliminated, and system currents remain balanced even if an 11% current imbalance is applied.
Figure 9. Experimental Transient Response after APF Connection. (a) Load Current $i_{Lu}$, active power filter current $i_{ou}$, dc-voltage converter $v_{dc}$, and system current $i_{su}$. Associated frequency spectrum. (b) Voltage and system waveforms, $v_{su}$ and $i_{su}$, $i_{sv}$, $i_{sw}$. (c) Current reference signals $i_{ou}$*, and active power filter current $i_{ou}$ (tracking characteristic).

Figure 10. Experimental Results for Step Load Change (0.6 to 1.0 p.u.). Load Current $i_{Lu}$, active power filter current $i_{ou}$, system current $i_{su}$, and dc-voltage converter $v_{dc}$.
7. CONCLUSION

Improved dynamic current harmonics and a reactive power compensation scheme for power distribution systems with generation from renewable sources has been proposed to improve the current quality of the distribution system. Advantages of the proposed scheme are related to its simplicity, modelling, and implementation. The use of a predictive control algorithm for the converter current loop proved to be an effective solution for active power filter applications, improving current tracking capability, and transient response. Simulated and experimental results have proved that the proposed predictive control algorithm is a good alternative to classical linear control methods. The predictive current control algorithm is a stable and robust solution. Simulated and experimental results have shown the compensation effectiveness of the proposed active power filter.

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