Parametric studies of ring and parallel coupled line resonators for matched bandstop filter design

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1. INTRODUCTION

In general, bandstop filters (BSF) are commonly used for rejecting unwanted blocking and interference signals in RF and microwave systems [1], [2]. It is well known that the planar technologies, particularly those using microstrip, suffer from low Q factor compared to non-planar technologies, such as coaxial and rectangular waveguides [3]. High notch depth and selectivity of bandstop filters are usually difficult to achieve with low Q factor of lossy resonator, unless multiple lossy resonators are placed in the design for higher n-order of bandstop filter. However, it tends to be physically large and complex.

A study issued in 2005 could successfully demonstrate an ideal infinite stopband attenuation of the matched bandstop, where high notch depth and selectivity can be produced with only two lossy low-Q resonators in microstrip technology [4]. Figure 1 presents the generalized model of matched bandstop filter using lossy resonator.

After the first prototypes from [4], other distributed elements of lossy resonators or different shapes (such as ring or coupled line) of matched bandstop filters have been proposed and reported by other researchers [5]-[12]. Besides, the matched bandstop filter was also realized by using lumped element type of resonator [13], [14].

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Recently, modern RF and microwave systems started tending towards cognitive operations thus, more tunable and switchable filters were conducted. For instance, a matched bandstop filter with the feature of switching between bandstop and all-pass was reported using ring resonator [15] and parallel-coupled resonator [16]. Furthermore, there were switchable matched bandstop to band-pass filter designs utilizing ring resonator [17] and parallel-coupled resonator [18]. Besides, the potential application of tunable matched bandstop filter in SPDT switch was discussed in [19]-[23].

In these matched bandstop filter designs, the key problem is the couplings of any microstrip resonators to the transmission microstrip line that have the variation or tolerance of coupling gap. As reported in [15], it was found that the bandstop response is very sensitive to the gap size of the coupled line. The smallest changes of coupling gap could significantly change the response. Unfortunately, the previous reported studies did not analyze and discusses the designing process of matched bandstop filter using lossy resonators. Therefore, in this paper, parametric studies of dual mode parallel coupled line and ring resonator for matched bandstop filter design are analyzed and discussed for helping and guiding other researchers who intend to deal with these type of matched bandstop filters.

![Generalized model of matched bandstop filter](image)

Figure 1. Generalized model of matched bandstop filter [4]

2. THEORETICAL OF MATCHED BANDSTOP FILTER

This is a simple analysis and discussion of attenuation response of matched lossy resonators. The theory of matched bandstop filter using lossy resonator was derived mathematically from mathematical model of allpass network [4]. Consider an even-mode and odd-mode analyses of matched bandstop filter, a transfer matrix of the symmetrical network is given by

\[
[T_e] = \begin{bmatrix}
Y_e + Y_o & 2 \\
Y_o - Y_e & Y_o - Y_e \\
2Y_o & Y_e + Y_o \\
Y_o - Y_e & Y_o - Y_e
\end{bmatrix}
\]

where \( Y_e \) is even-mode, and \( Y_o \) is odd-mode of admittance of the resonator. If \( Y_o = \frac{1}{Y_e} \), the general mathematical model of \( S_{21} \) of matched lossy resonator was rewritten as

\[
S_{21} = \frac{(1 - Y_e^2)Z_0}{(Z_0 + Y_e)(Z_0Y_e + 1)}
\]

Now consider the case where \( Y_e \) is a lossy circuit, \( Y_e = R + j\omega L + \frac{1}{j\omega C} \). Then, (2) was rewritten as

\[
S_{21} = \frac{\left(1 - \left( R + j\omega L - \frac{j}{\omega C}\right)^2\right)Z_0}{\left(Z_0 + \left( R + j\omega L - \frac{j}{\omega C}\right)\right)\left(Z_0\left( R + j\omega L - \frac{j}{\omega C}\right) + 1\right)}
\]
From (3), the resonant results when
\[ j\omega L - \frac{j}{\omega C} = 0 \] (4)
Rearrange (3) with (4), then we get
\[ S_{21} = \frac{(1 - R^2)Z_0}{(Z_0 + R)(Z_0R + 1)} \] (5)
Consider a normalized characteristic impedance where \( Z_0 = 1 \) and resistance of resonator, \( R = 1 \). Hence, the S-parameter of (5) becomes
\[ S_{21} = \frac{(1 - 1^2)1}{(1 + 1)(1 + 1)} = 0 \] (6)
or in decibel
\[ |S_{21}|^2\text{dB} = 20 \log_{10}(0) = \infty \text{ dB} \] (7)
where an infinite attenuation response was obtained in the matched lossy resonator. The detailed analyses of the attenuation response of the matched lossy resonators (parallel coupled line and ring resonator) are discussed in the next sections. Since there was no synthesis technique to obtain attenuation response based on the matches lossy resonator structures [9], [4], the parametric study technique was used for the attenuation response analysis. The ADS software was used for the parametric study by designing the matched lossy resonators in the schematic design tool.

3. RESULTS AND ANALYSIS
3.1. Parallel Coupled Line Resonator
For better understanding of the characteristics of matched lossy resonator using parallel coupled line structure, the analysis was begun with a conventional single resonator. The basic structure was reported in [24] for bandstop filter design, which is also known as L-shape resonator. It was coupled to the main microstrip line both electrically and magnetically.

As depicted in Figure 2(a), the single parallel coupled line resonator structure was coupled in parallel to the microstrip transmission line. The length of the parallel coupled line resonator was half wavelength, \( \lambda/2 \) at resonant frequency. The simulated frequency response \( (S_{21} \text{ and } S_{11}) \) is plotted in Figure 2(b), from which the desired resonator structure parameters were determined; resonator length, \( l = 21.3 \text{ mm} \) (resonated at 3.5 GHz), coupling spacing, \( S = 0.5 \text{ mm} \), and width of microstrip line, \( W = 2.9 \text{ mm} \).

![Figure 2. (a) A single parallel coupled line resonator, (b) the simulated frequency response](image-url)
It was observed that the simulated attenuation or notch of the resonator in Figure 2(b) was low, -7 dB at 3.5 GHz. The simulated return loss was -5.7 dB. This was due to the lossy type of resonator using microstrip transmission line. From the simulated frequency response, the 3-dB bandwidth was 175 MHz. Thus, the calculated unloaded Q factor was 40.

The notch of the parallel coupled line resonator was increased by cascading more than one resonator. As depicted in Figure 3(a), double parallel coupled line resonator structures were cascaded in series with microstrip transmission line. The parallel coupled line resonators were separated with k-inverter that had been realized using quarter wavelength, $\lambda/4$ at resonant frequency.

The simulated frequency response ($S_{21}$ and $S_{11}$) was plotted in Figure 3(b), from which the desired resonator structure parameters were determined; resonator length, $l_1 = 21.3$ mm (resonated at 3.5 GHz), $k_3$ length, $l_2 = 11$ mm (resonated at 3.5 GHz), coupling spacing, $S = 0.5$ mm, and width of microstrip line, $W = 2.9$ mm. As shown in Figure 3(b), the simulated notch of the cascaded two parallel coupled line resonator increased to -16.8 dB, while the return loss was -7.2 dB. From the simulated frequency response, the 3-dB bandwidth was 166 MHz. Thus, the calculated unloaded Q factor was 42.

Furthermore, based on the conventional parallel coupled line resonator structures that have been discussed in the previous paragraphs, notch or attenuation of the resonator could be enhanced by using matching lossy bandstop filter design proposed by [4]. Figure 4 is the desired dimension of matched parallel coupled line resonator operated at 3.5 GHz, where the resonator length, $l_1 = 21.3$ mm, length of k-inverter, $l_2 = 15.4$ mm (including microstrip bends), and width of microstrip line, $W = 2.9$ mm. The length of k-inverter, $l_2$ is the $k_3$ shown in generalized model of matched lossy resonator.

![Figure 3](image.png)

**Figure 3.** (a) A double parallel coupled line resonator, (b) the simulated frequency response

The parametric studies of the simulated frequency response ($S_{21}$ and $S_{11}$) were plotted in Figures 5 and 6 by varying the coupling spacing, $S_1$ and $S_2$ respectively in order to determine the best high notch ($S_{21}$) and matched return loss response ($S_{11}$). Take note that, according to generalized model of matched lossy resonator, the $k_1$ was realized by $S_1$, while the $k_2$ was realized by $S_2$. From literature, perfectly matched and very high notch response could be obtained with the proper selection of values of $k_1$ and $k_2$. 
Figure 4. Matched lossy resonator using parallel coupled line and its parameters

Based on Figures 5(a) and (b), the parametric studies of $S_{21}$ and $S_{11}$ were performed in the ADS software by varying $S_I$ without coupling spacing between resonators, $S_2$. The value of $S_I$ was varied from 0.1 mm to 2.5 mm. In this case, the circuit model in the ADS software was set without coupling of $S_2$ using a normal microstrip transmission line. The result showed that high notch was obtained by reducing the coupling spacing, $S_I$, when the electrical and magnetic field was increased. However, Figure 5(b) shows a highly unmatched response of return loss when $S_I$ was reduced. The matched return loss response could only be obtained by increasing the coupling spacing, $S_I$. Thus, there was a trade-off between high notch and matched return loss response when choosing the best $S_I$ value in parallel coupled line resonator design.

![Figure 5(a)](image1) ![Figure 5(b)](image2)

Figure 5. Parametric study of (a) $S_{21}$ and (b) $S_{11}$ with variation in $S_I$ without $S_2$

Meanwhile, in Figure 6(a) and Figure 6(b), parametric studies of $S_{21}$ and $S_{11}$ were performed by varying $S_2$ with fixed coupling spacing, $S_I = 0.5$ mm. The value of $S_2$ was varied from 1 mm to 16 mm. In this case, the circuit model in the ADS software had included the $S_I$ as the resonators must be coupled to the main microstrip transmission line.

![Figure 6(a)](image3) ![Figure 6(b)](image4)

Figure 6. Parametric studies of (a) $S_{21}$ and (b) $S_{11}$ with variation in $S_2$ with $S_I = 0.5$ mm
From the simulated result, it was found that a high notch with an acceptable matched return loss response was obtained at a certain value of $S_2$. In this parametric study, $S_2 = 8$ mm gave the highest attenuation, -29.8 dB (in Figure 6(a)) with an acceptable matched response of the return loss, -10.6 dB (in Figure 6(b)). From the simulated frequency response (for $S_2 = 8$ mm), the 3-dB bandwidth was 137 MHz, giving the calculated unloaded $Q$ factor was 51. The best matched return loss response was obtained when $S_2 = 4$ mm, which was -25.9 dB return loss, but the notch response ($S_{21}$) had slightly dropped to -18.5 dB. Thus, there is a trade-off between high notch and matched return loss response when choosing the best $S_2$ value in parallel coupled line resonator design. Therefore, based on these two simulated results in Figures 5 and 6, it was found that with careful design and proper circuit parametric study on the coupling spacing of $S_1$ and $S_2$, very high notch and matched return loss response were obtained.

3.2. Ring Resonator

As depicted in Figure 7, the matched lossy resonator using ring structure was side coupled to the microstrip transmission line. The total length of the matched ring resonator was full wavelength, $\lambda$, at resonant frequency. That means, for each length of $l_1$, the wavelength was $\lambda/4$, and it formed a square shape of ring resonator. Furthermore, according to [25], a ring resonator with side coupled to a microstrip line produces two closely spaced, but distinct resonant frequencies were identified due to the even mode and odd mode coupling. The perturbing stub, $l_3$, was employed at 135° of electrical length from input or output feed lines (Port 1 or Port 2) in order to gain flexibility of controlling the resonant frequency of odd mode coupling. Besides, it has been known that the ring resonator is a dual mode resonator [3]. Thus, in order to observe the dual mode response of ring resonator in this research work, the ring structure in Figure 7 was simulated in the ADS software without perturbing stub, $l_3 = 0$ mm, and all the width of resonator and transmission line shared the same width, $W_1 = W_2 = 2.9$ mm. The coupling spacing, $S$ was fixed at 0.5 mm, $l_1 = 9$ mm and $l_2 = 10$ mm (resonated at 3.5 GHz). In addition, according to [3], the asymmetrical feed lines (or side coupling) are used to the ring resonator so that two degenerate modes or splitting resonant frequencies can be exited in the ring resonator.

Thus, the simulated frequency response ($S_{21}$ and $S_{11}$) in Figure 8 shows two degenerate modes or splitting resonant frequencies at 3.59 GHz and 3.41 GHz. The simulated notches or attenuations were -10.6 dB (at 3.59 GHz) and -7.9 dB (at 3.41 GHz), while the simulated return loss of the two resonant frequencies were -3.9 dB (at 3.59 GHz) and -5.6 dB (at 3.41 GHz).

According to [25], the two distinct resonant peaks were identified as the even-mode (magnetic field) and odd-mode (electric field) coupling of the ring resonator to microstrip line. Hence, as depicted in Figure 8, the resonant frequency of 3.59 GHz was due to even mode coupling, while the resonant frequency of 3.41 GHz was due to odd mode coupling. As reported in [26], the even mode and odd mode couplings would take place if the induced magnetic or electric field is maximum at the resonator near the microstrip transmission line.
Parametric studies of ring and parallel coupled line resonators... (A.M. Zobilah)
Figures 10(a) and (b) show that the resonant frequency of odd coupling was shifted to lower frequency by increasing the length of the perturbed stub. Besides, the values of notch, $S_{21}$, and return loss, $S_{11}$, had been almost similar when the resonant frequency was shifted to lower frequencies.

In Figure 11, the parametric studies of $S_{21}$ and $S_{11}$ were performed by varying $W_2$ without perturbed stub, $l_3 = 0$ mm and with fixed coupling spacing, $S = 0.1$ mm. In this simulation, the value of $W_2$ was varied from 2.9 mm to 2 mm. It was observed that the resonant frequencies of both even and odd modes were shifted to the center frequency of ring resonator at 3.5 GHz by reducing $W_2$.

In Figure 11(a), the highest notch was obtained when $W_2 = 2.5$ mm, but by reducing the width lower than 2.5 mm, it lowered the notch response. This was due to the increase in coupling spacing, $S$, simultaneously with reduction of $W_2$, hence weakening the even mode and odd mode couplings. On the other hand, Figure 11(b) shows a matched response of return loss when the value of $W_2$ was increased. The return loss, $S_{11}$, began to show matched return loss response when $W_2 < 2$ mm, thus a trade-off between high notch and matched return loss response was found when choosing the best coupling spacing, $W_2$, in the ring resonator design.

Based on the simulated results in Figures 9, 10, and 11, it was found that a very high notch and matched return loss response were obtained with careful design and proper circuit parametric study on the coupling spacing, $S$, width at coupling lines, $W_2$, and perturbed stub length, $l_3$.

4. CONCLUSION

Parametric studies of dual mode parallel coupled line and ring resonators for matched bandstop filter design was discussed. For parallel coupled line, based on the two simulated results in Figures 5 and 6, it was found that with careful design and proper circuit parametric study on the coupling spacing of $S_1$ and $S_2$, very high notch and matched return loss response were obtained. In contrast, based on the simulated results in Figures 9, 10, and 11, it was found that a very high notch and matched return loss response were obtained with careful design and proper circuit parametric study on the coupling spacing, $S$, width at coupling lines, $W_2$, and perturbed stub length, $l_3$. Therefore, the crucial issue in the parallel coupled line and ring resonators is the variation or tolerance of coupling gap. The smallest changes of coupling gap could significantly change the response.
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