Frequent Itemsets Mining based on Concept Lattice and Sliding Window

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Abstract

In this paper, a frequent itemsets mining algorithm of data stream based on concept lattice and sliding window is presented. This algorithm mines frequent concepts for new inflowing basic window in batches in a sliding window and generates concept lattice Hasse diagram. With introduction into small support degree $\zeta$ and error factor $\varepsilon$ to do the pruning operations for non-frequent concept node, each connection point in the Hasse diagram contains the information of frequent itemsets and support degree. As the generation of Hasse diagram in the new basic windows, we integrate concept lattice vertically with the generated Hasse diagram and sliding window, and ultimately output all frequent itemsets through scanning all the graph nodes of Hasse diagram graph. The experimental results show that the proposed algorithm has a good performance.

Keywords: data steam, frequent patterns, sliding window, concept lattice

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1. Introduction

With the growing number of data applications, the data mining techniques have attracted widespread attention under environment of data stream. However, data stream has characteristics of continuous, unlimited, real-time, and un-prediction, and the traditional frequent pattern mining algorithms are difficult to deal with such data stream. Therefore, frequent pattern mining under the environment of data stream has become a challenging research direction. Some relevant algorithms are put forward successively, such as Sticky Sampling and Lossy Counting in the literature [1] gave an effective algorithm for solving a single frequent pattern by introducing the error factor $\varepsilon$, this algorithm can obtain the entire frequent itemsets of data stream by scanning data. The FP-Stream algorithm was presented in the literature [2]. This algorithm uses the Pattern-Tree structure with a similar FP-Tree prefix tree to store the potential frequent pattern information for the time window in the past, and solves the time sensitivities problem of historical data by the introduction of tilted time window techniques. Chang in the literature [3] proposed a mining frequent itemsets algorithm SW by making use of sliding window. The concept of frequent closed patterns was proposed by Pasquier in the literature [4], it is only to determine the accurate support rate of all frequent patterns, and the size is of smaller magnitudes of order than the frequent pattern set. Chi in the literature [5] provided closed frequent itemsets mining algorithm based on sliding window.

Since the theory of formal concept analysis was put forward according to the philosophy of "concept" thinking by Germany professor Wille since 1982 [6], its core data structure of the formal concept analysis theory is-concept lattice. Relevant researches have obtained rapid development, several research directions on the combination of concept lattice and data mining has gradually become a hot topic. Because the essence of concept lattice is a concept of hierarchical structure induced by a binary relation, it is very suitable for data analysis and rule extraction. According to the generated process of concept lattice by number of data records in data sets, its essence is a clustering process for concepts. And it is a very useful formal analysis tool. The concept lattice embodies the unification for the concepts of connotation and
denotation, it not only reflects the association between objects and attributes, but also contains the concept relationships between generalization instantiation. Therefore, it is very suitable to find the potential concept and knowledge with combinations with data mining applications.

At present, group of scholars at home and abroad have already studied the combined application of concept analysis and data mining, the main research directions focus on some quick concept lattice algorithms [7, 8], the association rule algorithms based on concept lattice [9, 10], the classification algorithms based on concept lattice [11], the relationships between the concept lattices and rough sets [12, 13], and other aspects.

There are few works about mining frequent itemsets in data stream based on concept lattice by access to domestic and foreign literature. Learn from previous researches on data stream mining and concept lattice, in this paper, we present a new frequent pattern mining algorithm DSCL in data stream based on sliding window and concept lattice. The proposed algorithm makes use of a core data structure concept lattice Hasse diagram in the formal concept analysis theory to store some potential frequent concept in the sliding window, as the sliding window updating and maintaining this structure in real time constantly, we can output the frequent itemsets.

2. Related Definitions

2.1. Sliding Window

Definition 1. Suppose I={i₁,i₂,...,iₙ} be a set of all data items, itemset X is a subset of complete data items I sub-sets (X ⊆ I), some items containing k items are k-itemsets. Transaction T is an itemset, data stream can be seen as a continuous arriving transaction sequence DS = {T₁, T₂, ..., Tₙ}. Let T₁ be the transactions of earliest arrival time in data stream, Tₙ be the latest arrival transactions in the data stream.

Definition 2. Let w represent the fixed size of basic sliding window, that is, there are only w recent transactions in the basic sliding window. Data stream DS can be segmented according to the number W, each w transactions correspond to as a sub-sequence data stream, that the corresponding size (or width) of the basic sliding window is w. The current basic sliding window is represented as: sw={T₁,T₂,...,Tₙ}, where sw indicates the basic sliding window, i is the current window number of the window (i.e., the i-th basic window). The sliding window SW consists of a continuous series of basic window swᵢ, which denotes as <sw₁, sw₂,..., swₖ>, sliding window contains the numbers of the window is the size of the sliding window, denoted by | SW | = k.

![Figure 1. Sliding Window](image)

Definition 3. Given a minimum support threshold ζ and error factor ε, suppose w denote the width of the sliding window SW, that SW contains number of transactions. fₛₚ(A) denotes the support count of pattern A in the sliding window SW. For pattern A, if there is fₛₚ(A)≥(ζ - ε)w, then A is a frequent pattern in the sliding window SW; if there is fₛₚ(A) > ε w, then A is a critical frequent pattern in the sliding window SW; if there is fₛₚ(A)≤ε w, then A is a non-frequent pattern in the sliding window SW; for the basic window sw also has the same definition as above.

2.2. Concept Lattice

In the formal concept analysis, it can be understood as follows, the extension of a concept C is a set of all objects that belong to the C, the common feature or attribute set of all
these objects is called the connotation of the concept C, and each concept in concept lattice is a set of objects of the greatest common properties. All concepts together with the relationships of generalization/instantiation form the concept lattice. The concept lattice is the core data structure of formal concept analysis theory, the corresponding Hasse diagram realize data visualization.

**Definition 4:** A formal context (Context) is a triple $K = (G, M, I)$, where $G$ is a set of objects, $M$ is a set of attributes, $I$ is a binary relation between the $G$ and $M$, i.e. $I \subseteq G \times M$, $g I m$ denotes it exists a relationship $I$.

**Definition 5:** In the formal context $K$, a binary groups $(A, B)$ from $G \times M$ exists the following two properties:

1. $B = f(A)$, where $f(A) = \{m : (m \in M) \land (\forall g \in A \subseteq G, g I m)\}$.
2. $A = g(B)$, where $g(B) = \{g : (g \in G) \land (\forall m \in B \subseteq M, g I m)\}$.

In the formal context $K$, $(A, B)$ is called as a concept, where $B$ is referred to as intent of the concept (Intent), and $A$ is called the extension of the concept (Extent).

**Definition 6:** A partial order relation between the concept nodes is established. Given $C_1 = (A_1, B_1)$ and $C_2 = (A_2, B_2)$, then $C_1 > C_2 \iff B_1 \subset B_2 \iff A_1 \supset A_2$, the leading order means $C_1$ is the parent node of $C_2$ or the generalization. If concepts $C_1 = (A_1, B_1)$ and $C_2 = (A_2, B_2)$ satisfy $A_2 \subset A_1$, and there does not exist the concepts $(A,B)$ such that $A_2 \subset A \subset A_1$; then $C_1$ is called the direct super-concept of $C_2$, $C_2$ is a direct sub concept of $C_1$, referred to as $(A_1, B_1) > (A_2, B_2)$. The linear diagram of concept lattice is generated based on the partial order relation, that is Hasse diagram.

**Definition 7:** Given a set of objects $G$, and a set of attributes $M$, a binary relation $I \subseteq G \times M$ (here $(g, m) \in I$ is called as "object $g$ has attribute $m".

**Definition 8:** For the concept $C(X, Y)$, $C(\{X\}, Y)$ is quantized by the concept $C$, and $C$ is the real concept of $C$. $|X|$ is the cardinality of the epitaxial $X$, the posed lattice is quantified by quantitative concept, which is quantitative concept lattice.

**Definition 9:** Given concept $C(A, B)$, $B \in M$; given a threshold $\text{minsup} \in [0, 1]$, the support degree of attribute set $B$ in forms background $K$ is $\text{sup}(B) = \frac{|\{g \in G| (\forall m \in B : (g, m) \in I)\}|}{|G|}$, if $\text{sup}(B) \geq \text{minsup}$, then $B$ is called the frequent attribute set (content), and $C$ is a frequent concept. That if the connotation of concept is frequent, then the connotation is called as the concept of frequent connotation, which is also called as frequent concept, $\text{sup}(C) = \frac{|\{g \in G| (\forall m \in B : (g, m) \in I)\}|}{|G| \geq \text{minsup}}$ where $|A|$ is the epitaxial base of concept $C$, $|G|$ is the total number of transactions in the database $D$.

3. DSCL Algorithm

3.1. The Descriptions of Algorithm

Algorithm DSCL divides data stream into some data blocks of equal length, each data block is as a basic window $sw$, each window contains the number of transactions $w$, and $k$ consecutive basic windows are composed of a sliding window $SW$. The algorithm generates a Hasse diagram after the first window entering into the sliding window, and after each new window entering into the sliding window the new Hasse diagrams are generated, and they merge vertically and reconstruct with previous Hasse diagrams in real-time. After completing the establishment and consolidation of Hasse diagram for basic window and generate new Hasse diagram that are reference to error factor $\varepsilon$ and the minimum support threshold $\zeta$ to filter out non-frequent concept (pruning) and to reconstruct the sides of Hasse diagram. The Algorithm just need to handle and store the critical frequent concept set of each basic window, it does not contain non-frequent concept node. Therefore, this algorithm greatly reduces the processing time and the amount of data storage. It consists of four main parts: the initialization of window, the stage of window sliding, the pruning of window Hasse diagram and the merger of window Hasse diagram.

3.2. Pseudo Codes

Algorithm 1: DSCL
Input: The basic windows $sw_1$, $sw_2$, $sw_3$, ..., $sw_w$ of data stream, the minimum support degree $\zeta$, the error factor $\varepsilon = x \zeta$, the size of sliding window $k$, the size of basic window size $w$.

Output: the frequent concept lattice Hasse diagram.

Step 1:
1. $i=1$; // $i$ is the identification of basic $sw_i$
2. $n=0$; // $n$ is the count of the current sliding window SW containing basic $sw_i$
3. $\varepsilon = x \zeta$ // error factor, $x$ is adjustable
4. $\minsupw = \varepsilon w$; // The critical support count of basic window
5. $\minsupk = \varepsilon k w$; // The critical support count of sliding window
6. $\minsupn = \varepsilon (n+1) w$; // The critical support count of sliding window for $n+1$ basic windows
7. $\text{Hall}_i = \emptyset$; //Current Hasse diagram $\text{Hall}_i$ is empty
8. $\text{Flag} = false$; // Whether the sliding window is full window

Step 2: Input basic sliding window $sw_i$, use 0,1 to indicate whether the transaction owns the attribute and generate a formal context matrix.

Step 3: $sw_i => \text{Hasse diagram } H_i$; // use the improved algorithm to generate concept lattice in batch $sw_i$ of Hasse diagram $H_i$;

Step 4: IF $n > k$
1. $\text{Flag} = true$; // $\text{Flag} = true$ is full window
END IF

Step 5: IF $\text{Flag} = false$ // $\text{Flag} = true$ is full window
1. IF $H_{\text{Hall}_{i-1}} \neq \emptyset$
   1. $H_{\text{Hall}_{i-1}} + H_i \Rightarrow H_{\text{Hall}_{i}}$; // call the improved vertical integration of concept lattice algorithm to combine and generate the Hasse diagram $H_{\text{Hall}_{i}}$
   2. $\text{Let } \minsupn = \varepsilon \zeta (n+1) w$; // the support count of the sliding window for current $n+1$ basic windows
   3. $\text{DeleteConceptLattice}(H_{\text{Hall}_{i-1}}, \minsupn)$; // Delete no-frequent concepts
   4. $n=n+1$; // Record the number of basic windows entering into the sliding window
   ELSE IF $H_{\text{Hall}_{i-1}} = \emptyset$
   1. $H_{\text{Hall}_{i}} \Rightarrow H_{\text{Hall}_{i+1}}$; //Initialize $H_{\text{Hall}_{i}}$ is $H_i$
   END IF
ELSE
1. delete $H_{\text{Hall}_{i-1}}$ From $H_{\text{Hall}_{i}}$; // Delete Hasse diagram $H_{\text{Hall}_{i-1}}$ of basic window $sw_{i-1}$ in $H_{\text{Hall}_{i-1}}$
2. $H_{\text{Hall}_{i-1}} + H_i \Rightarrow H_{\text{Hall}_{i}}$; // call the vertical integration of improved concept lattice algorithm to generate the Hasse diagram $H_{\text{Hall}_{i}}$ of combining $H_i$ and $H_{\text{Hall}_{i-1}}$
3. $\text{DeleteConceptLattice}(H_{\text{Hall}_{i}}, \minsup_k)$; // To delete no-frequent concepts
END IF

Step 6: $i=i+1$, turn to Step 2. // Get the next basic window $sw_{i+1}$

Algorithm 2: $\text{DeleteConceptLattice} (H , \minsup_{\text{Num}})$
Input: Hasse diagram $H$ of one concept lattice Minimum support count $\minsup_{\text{Num}}$
Output: Hasse diagram $H'$.

Begin
1. For each $C \in H$ // $C$ is a node of $H$
   1. If $\sup(C) \leq \minsup_{\text{Num}}$
   2. $\text{Delete } C \text{ from } H$; // Delete no-frequent concepts $C$ from $H$, do the pruning operation
   END For
   2. For each $C \in H$
   3. $\text{Re_Add edge } C \Rightarrow H$; // Reconstruct side for each concept node
   END For
END

3.3. Instance of Verification
The preceding 16 transactions in data stream $DS$ determine the formal context $K$ as shown in Table 1, $w=4$, $k = 3$, $\zeta = 30\%$, $\varepsilon =0.33 \zeta$.
Table 1. Formal Context

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</table>

Step 1: // Initialize parameters

\[ \text{i}=1; \] // i is the identification of basic sw_i
\[ \text{n}=0; \] // The count of basic window containing some basic windows
\[ \varepsilon=0.3, \kappa=0.33; \] // error factor
\[ \text{Minsupw}=0.4; \] // The critical support count of basic window
\[ \text{Minsupk}=1.2; \] // The critical support count of sliding window
\[ \text{Minsupn}=0.4; \] // The critical support count of only one basic window
\[ \text{Hall}_0=\phi; \] //current Hasse diagram Hall is empty
\[ \text{Flag}=false; \] //whether the sliding window is full

Step 2: The sliding window SW_i is empty, which is a non-full window. The inflowing data of the basic window SW_i is T_1, T_2, T_3, T_4. We use 0,1 to indicate that the transaction whether has this attribute and generate a formal context matrix, such as the first to fourth row in Table 1.

Step 3: The improved batch algorithm let sw_1 generate Hasse diagram denoted as H_1, due to Minsupw=0.4, which is less than the minimum support count 1 of the concept nodes in H_1, and we do not need to call Delete Concept Lattice (H_1, Minsupw), the result of this step is shown in Figure 2.

Figure 2. H_1 Diagram

Figure 3. H_all-1 Diagram

Figure 4. H_2 Diagram

Step 4: Due to n=0; thus n>=k does not satisfy, Flag=false, the current sliding window is not a full window.

Step 5: Because Flag = false and Hall_0=\phi, thus H_1=> Hall_1, the current concept lattice Hall_1 of sliding window, which shown in Figure 3.

Step 6: i= i +1, turn to Step 2, as described above steps, continue to complete the input of sw_2 and sw_3 the results are as follows:

The inflowing data of the basic window sw_2 is T_5, T_6, T_7, T_8, and the inflowing data of the basic window sw_3 is T_9, T_10, T_11, T_12, such as the fifth to eighth row in Table 1, the ninth to twelfth row in Table 1.

The generated Hasse_2 diagram of sw_2 is denoted by H_2, as shown in Figure 4; combine H_2 and Hall_1 to generate the H_all_2 shown in Figure 5, because Minsupn=0.8 is less than the minimum support count of concept lattice in H_all_2 diagram. Thus it does not call Delete Concept Lattice (H_all_2, Minsupn);
The generated Hasse diagram of \( sw_3 \) is denoted by \( H_3 \), as shown in Figure 6; combine \( H_3 \) and \( H_{all-2} \) to generate the \( H_{all-3} \) shown in Figure 7, because \( \text{Minsup} = \varepsilon (2+1) \) \( w=1.2 \) is less than the minimum support count of concept lattice in \( H_{all-3} \) diagram. Thus it does not call DeleteConceptLattice (\( H_{all-3}, \text{Minsup} \)), and delete the concept nodes of non-frequent concept lattice, and generate \( H_{all-3} \) in Figure 8.

\[
\text{Step 7:} \quad i = i + 1, \quad \text{Step 2-Step 6 are repeated, continue to complete the input and processing of} \quad sw, \quad \text{the results are as follows: the inflowing data of basic window} \quad sw, \quad \text{is} \quad T_{13}, T_{14}, T_{15}, T_{16}, \quad \text{generate a formal context matrix in the in the 13th to the 16th row shown in Table 1.}
\]

The generated Hasse \( H_4 \) diagram denoted by \( H_4 \), as shown in Figure 9; and execute to Step 4, since \( n=k=3 \), so Flag=true; and then perform Step 5, delete firstly the concept nodes in \( H_4 \), from \( H_{all-3} \) and generating \( H_{all-4} \), as shown in Figure 10. Then, call the improved vertically merging algorithm of concept lattice and combine \( H_4 \) and \( H_{all-3} \) to generated Hasse diagram \( H_{all-4} \), as shown in Figure 11; and call DeleteConceptLattice (\( H_4, \text{Minsup} \)) to delete non-frequent concept node in \( H_{all-4} \) and generate \( H_{all-4} \), the final result show in Figure 12.

\[
\text{Up to this step so far, the number of size of sliding window containing the basic windows, then the sliding window is full.}
\]

\[
\text{Figure 5.} \quad \text{H}_{all-2} \quad \text{Diagram}
\]

\[
\text{Figure 6.} \quad H_3 \quad \text{Diagram}
\]

\[
\text{Figure 7.} \quad H_{all-3} \quad \text{Diagram}
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\[
\text{Figure 8.} \quad H_{all-3} \quad \text{Diagram}
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\[
\text{Figure 9.} \quad H_4 \quad \text{Diagram}
\]

\[
\text{Figure 10.} \quad H_{all-3}
\]
Step 8: \( i = i + 1 \), repeat Step 2-6, and continue to complete the input and processing of \( \text{sw}_5, \text{sw}_6, \ldots, \text{sw}_n \).

4. Experimental Analysis

Because FP-stream algorithm has good time efficiency, we select the FP-stream as a comparison algorithm. The experimental environment is a PC machine of Windows Server 2003 operating system, I7 2.0G 64-bit quad-core eight lines into the processor, 8G memory, and the program runs on the JAVA SDK1.4.2 environment. The experiments [14] employ the data set T1016D100K generated by IBM synthetic data generator, where the total number of transactions are100,000, the average transaction length is 10, the average length of the potential frequent itemsets is 6, this data set contains different item number 1000. The experiments make a comparison with Algorithms FP-stream and DSCL, not considering the read time of data. Figure 13 presents a comparison of mining time consumption as the number of transactions of the sliding window change under the premise of the conditions that the window size \( w \) changes, the minimum support \( \zeta \) is 0.003, the error factor is 0.1 \( \zeta \); Figure 14 shows a comparison of memory consumption as the minimum support \( \zeta \) changes between Algorithms FP-stream and DSCL under the premise of the conditions that the window size \( W = 1000 \), the error factor takes 0.1 \( \zeta \).

The experiments have demonstrated the solving efficiency is similar between the DSCL algorithm and the FP-stream algorithm based on sliding time window and concept lattice. A good performance of this algorithm is to use Hasse diagram of the concept lattice to indicate frequent concept sets, the next is to compress the size of the concept lattice efficiently under the case of ensuring the integrity of information followed by the oriented concept lattice pruning strategy, greatly reduces the search range of the algorithm and improve the space-time complexities of the algorithm.
5. Conclusion

In this paper, a new frequent pattern mining algorithm DSCL in data stream based on sliding window and concept lattice, due to it employs a core data structure concept lattice Hasse diagram to store the potential frequent concept of the sliding window in the formal concept analysis theory, and use pruning strategy aiming for concept lattice in the generated process of basic window and sliding window, delete the non-frequent concept in the concept lattice. Because the scale after pruning concept lattice is much less than the corresponding scale of concept lattice, thus it greatly reduce the search scope of solving the frequent itemsets, overcome the drawback of previous construction algorithm on the concept lattice, and improve the space-time performance of solving the frequent itemsets based on concept lattice. The experimental results show that DSCL algorithm has a better time and space complexity. In this paper, we make an experimental under the fixed attributes of experimental data set. Our future research work is to the construction of concept lattice based on sliding window under the case that attributes increase or decrease around the concept solved oriented data flow, and to carry out the algorithm on merging vertically and horizontally, and to mine the frequent patterns and characteristics rules in the case of ensuring the performance of space and time complexities.

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