Optimal Selection of UPFC Parameters and Input Controlling Signal for Damping Power System Oscillations

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Abstract
Unified power flow controller (UPFC), as one of the most important FACTS devices, can be used to increase the damping of power system oscillation. The effect rate of this controller on increasing oscillation damping depends on the appropriate selection of input controlling signal, optimal selection of UPFC controlling parameters, and its proper position in power system. In this paper, the capability of different UPFC inputs is studied by utilizing singular value decomposition (SVD) method and the best UPFC input controlling signal is selected. Supplementary control parameters are also optimally selected by PSO algorithm. This method’s accuracy is simulated on a single-machine system connected to infinite bus.

Keywords: PSO algorithm, unified power flow controller (UPFC), low frequency oscillations, FACTS devices

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1. Introduction
Power system oscillations are the important subject that should be considered in power systems. The frequency of these oscillations is between 0.2 and 3 Hz; if they are not damping, their range will gradually increase and may endanger the system's stability [1, 2]. For damping of power system oscillations and increasing the system's oscillation stability, it is both economical and effective to install power system stabilizer (PSS) [3, 4]. Nevertheless, PSSs have some limitations and are not the solution by themselves. Flexible AC transmission system (FACTS) devices can cause a substantial increase in power transfer limits during steady state through the modulation of bus voltage, phase shift between buses, and transmission line reactance. FACTS devices are among the tools that have a very important rule in damping power system oscillations. Unified power flow controller (UPFC), as one of the most important FACTS devices, can control the power system parameters such as terminal voltage, line impedance, and phase angle.

Performance analysis and control synthesis of the UPFC require its steady-state and dynamic models. A 2-source UPFC steady-state model including source impedances is suggested in [5]. Wang developed two models of UPFC [6-8] in 1999, which have been linearized and incorporated into the Phillips-Heffron model. Using input controlling signals and appropriate parameters, it can be also efficient in damping the system oscillations [9]. The authors of [10] employed the real-coded genetic algorithm to optimize the damping controller parameters of the UPFC. In [11], bacterial foraging was used for the UPFC lead-lag type of controller parameter design. The imperialist competitive algorithm (ICA) has been used in a variety of research areas [12-16].

One of the important issues, in study and design of UPFC POD controllers, is an adequate input signal for controller. In this paper, singular value decomposition (SVD) method for selection of most suitable control input signal of UPFC to achieve effective damping of electromechanical mode of oscillation, has been presented. UPFC dynamical model is considered using Heffron-Phillips model to obtain its optimal controlling parameters. For signal controlling selection which has maximum effect on the damping of electromechanical oscillations, singular value decomposition (SVD) method is used. Supplementary optimal controlling parameters are also selected using PSO optimization method.
2. Research Method

Figure 1 shows a single-machine infinite-bus (SMIB) power system equipped with a UPFC. Static excitation system (IEEE-STIA type) and four-story turbine with appropriate governor are considered. System parameters and nominal performance conditions are presented in Appendix. As shown in the figure, UPFC consists of a parallel transformer (ET), a series transformer (BT), two three-phase voltage source inverters based on GTO, and a DC link capacitor. Voltage source inverters generate voltage with controllable phase angle and amplitude. For UPFC, there are four modulation indexes, $m_{SH}$ (amplitude modulation index for parallel inverter), $\delta_{SH}$ (phase angle of parallel inverter), $m_{SE}$ (amplitude modulation index for series inverter), and $\delta_{SE}$ (phase angle of series inverter) controlling signals. $i_t$ is armature current, $V_b$ is voltage of infinite bus, $V_{BT}$ is voltage of parallel transformer, $V_{BT}$ is voltage of series transformer, and $i_{TL}$ is parallel branch current.

By writing the dynamic equations for UPFC and system, we can linearize the obtained nonlinear equations using Taylor’s expansion around a specific operating point and have the following linear model:

$$
\Delta \delta = \omega_p \Delta \omega \\
\Delta \omega = (\Delta P_m - \Delta P_e - D \Delta \omega)/M \\
\Delta E' = (\Delta E_{ta} - (X_d - X'_d) \Delta i_d - \Delta E'_d)/T_d \\
\Delta E_{ta} = (K_A (\Delta V_{ref} - \Delta V_t + \Delta u_{pss}) - \Delta E_{ta})/T_A \\
\Delta V_{dc} = K_f \Delta \delta + K_b \Delta E' + \Delta \delta E_{ta} + K_c \delta_{SH} + K_c \delta_{SE} + K_c \delta_{SH} + K_c \delta_{SE} + K_c \delta_{SH} + K_c \delta_{SE}
$$

In these equations, $K_{vu}$, $K_{ve}$, $K_{qu}$, $K_{qe}$, and $K_1 - K_9$ are linearization constants that can be written in a parametric form. Accordingly, we can show the power system in the state-space model as follows:

$$X = AX + BU$$

Matrices $A$ and $B$ are state and input matrices, respectively. State vector $X$ and input vector $U$ are defined as follows:
\[
X = [\Delta \delta \ \Delta \omega \ \Delta E'_q \ \Delta E'_{fd} \ \Delta V_{dc}]^T \\
U = [\Delta u_{pss} \ \Delta m_{SH} \ \Delta \delta_{SH} \ \Delta m_{SE} \ \Delta \delta_{SE}]^T
\] (7) (8)

Linearized dynamic model of the state–space representation is shown in Figure 2, in which the stabilizer input of power system \([U_{pss}]\) and only one UPFC input control are shown. It should be considered that constants \([K_p, K_q, K_v, \text{and } K_u]\) shown in the figure are row vectors that can be defined as follows:

\[
K_{pu} = [K_{psH} \ K_{psE} \ K_{psE} \ K_{psSE}] \\
K_{qu} = [K_{qsH} \ K_{qsE} \ K_{qsE} \ K_{qsSE}] \\
K_{vu} = [K_{vsH} \ K_{vsE} \ K_{vsE} \ K_{vsSE}] \\
K_{cu} = [K_{csH} \ K_{csE} \ K_{csE} \ K_{csSE}]
\] (9) (10) (11) (12)

2.1. UPFC Supplementary Controller

For effective damping increase, supplementary control function helps UPFC via improving its UPFC control function. Supplementary controller's block diagram is shown in Figure 3 [9]. In this block diagram, \(T_w\) is wash-out time constant, \(T_1\) and \(T_2\) are lead time...
constant, \( T_3 \) and \( T_4 \) are lag time constant, and \( K \) is controller gain. Controlling parameters should be selected so optimally that have maximum effect on damping power system oscillations. In this research, these parameters are optimally selected using PSO algorithm.

\[
\Delta \omega \xrightarrow{\frac{T_{WS}s}{1 + T_{WS}}} K \xrightarrow{\frac{1 + T_1s}{1 + T_2s} \times \frac{1 + T_3s}{1 + T_4s}} \Delta u
\]

**Figure 3. Block diagram of UPFC supplementary controller.**

### 2.2. Optimal Design of UPFC Controlling Parameters

For optimal selection of stabilizing parameters in order to convert the problem into an optimization problem, a criterion function is selected based on specific values, which is then adjusted to increase damping factor or rate related to specific electromechanical values. The objective function can be defined as follows:

\[
j = \min(\xi) \quad (13)
\]

\[
\xi = \frac{|\text{Real}(EM)|}{\text{Real}(EM)^2 + \text{Imag}(EM)^2} \quad (14)
\]

Where \( \xi \) is damping rate of the mode related to specific electromechanical value (EM). It is clear that the objective function identifies the minimum damping rate of electromechanical modes at all operation points. Thus, we can increase damping rate of electromechanical modes and, accordingly, system damping by maximizing the objective function. So, we will have an optimization problem with the following constraints:

\[
K_{2i} \leq K_{3i} \leq K_{3i}^{\max} \quad (15)
\]

\[
T_{1i}^{\min} \leq T_{1i} \leq T_{1i}^{\max} \quad (16)
\]

\[
T_{2i}^{\min} \leq T_{2i} \leq T_{2i}^{\max} \quad (17)
\]

\[
T_{3i}^{\min} \leq T_{3i} \leq T_{3i}^{\max} \quad (18)
\]

\[
T_{4i}^{\min} \leq T_{4i} \leq T_{4i}^{\max} \quad (19)
\]

Optimal parameters of UPFC supplementary controller are obtained using PSO algorithm. Table (1) shows the numeral values of optimal parameters:

<table>
<thead>
<tr>
<th>( k )</th>
<th>( T_1 )</th>
<th>( T_2 )</th>
<th>( T_3 )</th>
<th>( T_4 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>97.7</td>
<td>0.584</td>
<td>0.298</td>
<td>0.2468</td>
<td>0.4239</td>
</tr>
</tbody>
</table>

### 3. Investigating Controllability Using Singular Value Decomposition (SVD)

According to Figure 2, it is found that the controlling stabilizer output can be applied to different inputs, i.e. \( \delta_{SH}, m_{SE}, \delta_{SE} \) and \( m_{SH} \) of UPFC. For selecting the input with maximum effect in the control of electromechanical modes in different operation conditions, singular value decomposition (SVD) method can be used [17]. In mathematical terms, if \( G \) is an \( m \times n \) complex matrix, there are \( W \) and \( V \) matrices with \( m \times n \) and \( n \times n \) dimensions such that the following relation is established:
G=W\sum V^H

(20)

Where \( \sum = \begin{bmatrix} \Sigma_1 & 0 \\ 0 & 0 \end{bmatrix} \); this is \( m \times n \) matrix and \( \Sigma_1 \) is defined as

\[
\Sigma_1 = \begin{bmatrix}
\sigma_1 & 0 & \cdots & 0 \\
0 & \sigma_2 & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & \sigma_r
\end{bmatrix}
\]

Where \( r = \min\{m,n\} \) and \( \sigma_1, \sigma_2, \ldots, \sigma_r \) are singular values of G matrix that are located in \( \Sigma_1 \) diagonal matrix in a descending order (\( \sigma_1 \geq \sigma_2 \geq \ldots \geq \sigma_r \)). Matrix B can be written as \( B = [B_1, B_2, B_3, B_4] \), where each \( B_i \) represents a column of matrix B and is in proportion to the \( i^{th} \) input. The minimum singular value of the matrix \([\lambda - A, B_i]\) indicates the capability of the \( i^{th} \) input to control the mode associated with the eigenvalue \( k \). Thus the minimum singular value of the matrix \([\lambda - A, B_i]\) corresponding to all four inputs parameters of UPFC, i.e., me, mb, de, db can be calculated and thus the most effective input parameter out of all four input parameters are identified.

Figure 4 shows the variations of MSV, DCT corresponding to all four control input parameters of UPFC with operating points for a range of loading conditions from 0.3 to 1.6 pu. According to this figure, \( \delta_{SE} \) and \( m_{SE} \) possess the highest SVD. Thus, they have maximum controllability to dampen the electromechanical modes of the power system. According to the figure, the following points are defined:

1. Controllability of \( \delta_{SE} \) signal is the highest.
2. Controllability of all four controlling signals is increased with load increase.

![Figure 4. Variation of SVD with load for UPFC control signal](image)

4. Simulation Results
To assess the effectiveness of the proposed stabilizers, the system eigenvalues are obtained and a disturbance increase of 25% in the mechanical input power is considered in order to obtain the dynamic responses. The system eigenvalues with and without the controllers are given in Table 2. It is clear that the system without the controllers is unstable. However, the proposed controllers dramatically stabilize the system. \( \delta_{SE} \) as the best input controlling signal of UPFC provides maximum damping ratio in the oscillating mode. System behavior due to the utilization of the proposed controllers was tested by applying a 25% step increase in mechanical...
input power at $t = 1$ s. The system response to this disturbance for speed deviation, and electrical power deviation with four controllers, as well as without controllers, are shown in Figures 5-8.

Table 2. The system's eigen values with and without UPFC controllers

<table>
<thead>
<tr>
<th></th>
<th>System without UPFC</th>
<th>$\delta_{SE}$</th>
<th>$m_{SE}$</th>
<th>$m_{SH}$</th>
<th>$\delta_{SH}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.39 ± 5.17i</td>
<td>-6.88 ± 10.89i</td>
<td>-4.12 ± 9.10i</td>
<td>-3.66 ± 12.72i</td>
<td>-0.079 ± 11.49i</td>
</tr>
<tr>
<td></td>
<td>-0.076</td>
<td>0.54</td>
<td>0.41</td>
<td>0.27</td>
<td>0.007</td>
</tr>
</tbody>
</table>

Figure 5. System's dynamic response with controller $\delta_{SE}$ : (a) Generator's output active power (pu), (b) Generator's velocity variations (pu). Solid line: $\delta_{SE}$ controller, dash line: without controller.

Figure 6. System's dynamic response with controller $m_{SH}$ : (a) Generator's output active power (pu), (b) Generator's velocity variations (pu). Solid line: controller $m_{SH}$, dash line: without controller.
It can be seen that the proposed objective function-based optimized UPFC controller has good performance in damping low-frequency oscillations and stabilizes the system quickly. Furthermore, from the above conducted test, it can be concluded that the $\delta_{SE}$-based damping controller is superior to the other damping controller, which confirms the results of the singular value decomposition analysis carried out for the UPFC input signals in Figure 4.

5. Conclusion

In this paper, performance improvement of dynamic stability was investigated by UPFC controller. Using PSO optimization method, UPFC damping control parameters were optimally selected. For studying the controllability of four controlling signals in UPFC, single value decomposition (SVD) method was used. According to SVD analysis, it was found that the controlling signal $\delta_{SE}$ had maximum controllability for the damping of the power system's electromechanical oscillations. Analysis of eigen values and simulation results of single-machine system connected to infinite bus using MATLAB software properly showed the effect of this proposed method.
References


