A Neural Network Based MPPT Technique Controller for Photovoltaic Pumping System

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ABSTRACT
The article proposes a novel method using the artificial neural network (ANN) for the improvement of the performances of a photovoltaic system composed of a photovoltaic (PV) array, an inverter, a motor asynchronous and a centrifugal pump. For this type of system, different optimization strategies have been proposed to improve the operation of the PV system efficiency, i.e. the PV generator is forced to operate at its maximum power point “MPPT”, generally, by the insertion of DC/DC boost converter between the photovoltaic array and the inverter. In this work we propose an approach, where optimization is realized without needing adding a DC/DC converter to the chain, using field-oriented control through the monitoring of the voltage-fed inverter frequency. The motor is also ensured in all insolation conditions. A multilayer feed forward perception type NN is proposed for MPPT control, and the back-propagation algorithm is used for training. The performances of the drive with ANN-based MPPT are excellent. The maximum power point (MPP) can be easily obtained to frequency-controlled drive.

Keyword:
PV Pumping System
Field-oriented control
MPPT
Neural Network
Performances

1. INTRODUCTION
The Saharan medium by its arid nature and the availability of solar immense can return the application of the water pumping via photovoltaic (PV) solar pumping, like a very important and the most attractive operation in the agricultural and industrial domains.

During the day, the speed of the motor asynchronous depends on the temperature and the quantity of the solar radiation that is fallen on the photovoltaic panels to extract the maximum power. This latter, is obtained by the proper adjustment of the inverter frequency (by increase or decreasing) instead of the MPPT circuit (maximum power point tracker), inducing a total improvement of the efficiency of the system without need adding a DC/DC converter to the chain. On the other hand, the flow daily and the efficiency of the motor-pump for a total head (HMT) depend on the speed (related to the stator frequency) if we considered that the number of stages is fixed (i.e Standard Centrifugal Pump, SCP) [1], [2]. For example, for a given speed, the pump functions at an operation point. If irradiance decreases, that involves a reduction speed; the system operating point is determined by the intersection point of the (Q, H) characteristics of the motor-pump.

The temperature and the radiation have random variation nature. By applying the technique of MPPT, the efficiency of the system rises whatever is the solar radiation value and the temperature of the environment. This technique was applied by different means [3]. In this study, we execute this technique with the use of artificial neural network (ANN). The application of ANN is recently growing in photovoltaic system. A feedforward ANN implements nonlinear input-output mapping. A back propagation type...
feedforward ANN is trained with the databases generated by a procedure that evaluated on a field-oriented controlled induction motor drive, it explains in detail in §3. The back propagation training algorithm needs only inputs and the desired output to adapt the weight [4].

2. SOLAR PUMPING SYSTEMS

The photovoltaic system is constituted of a self-piloted asynchronous motor operating a centrifugal load. The unit is fed by solar cells through an inverter. Pumping without intermediate power storage enabled us to have a simpler photovoltaic system, more reliable; maintenance-fee is less expensive than a system with battery [5].

The system to be investigated is an immersed centrifugal motor-pump SP5A7 (nominal speed 2860rpm for an industrial frequency equalizes with 50Hz).

Figure 1 shows the block diagram of a closed loop field-oriented controlled (FOC) induction motor drive incorporating the proposed ANN-based MPPT controller. The command voltage \( \begin{bmatrix} V_{ds} \\ V_{qs} \end{bmatrix} \) is generated from the frequency or speed \( \omega \) command (irradiance \( G \) and temperature \( T_a \) dependents).

![Figure 1. Field-oriented control of induction motor showing neural network based implementation](image)

2.1. Photovoltaic array model

Some authors have proposed more sophisticated models that present better accuracy and serve for different purposes. The basic equation from the theory of semiconductors that mathematically describes the I–V characteristic of the PV array, equation (1) describes the single-diode model presented in Figure 2 [6], [7].

![Figure 2. Single-diode model of the theoretical PV cell and equivalent circuit of a practical PV device including the series and parallel resistances](image)

\[
I = I_{ph} - I_D - I_{sh} \quad (1)
\]

\[
I_{ph} = N_p I_0 (1 + p_2 \Delta T) \quad (2)
\]

\[
I_p = N_p I_0 \left[ \exp \left( \frac{e_0 (V + \frac{N_q R_s}{N_p})}{A N_e e^2 N_q R_T c} \right) - 1 \right] \quad (3)
\]

\[
I_{sh} = N_p \frac{V + \frac{N_q R_s}{N_p}}{N_q R_{sh}} \quad (4)
\]

When:

\[
p_1 = \frac{I_{phref}}{E_{ref}} = \frac{(R_s + R_{sh}) I_{cref}}{R_{sh} E_{ref}} \quad (5)
\]
\[
p_2 = \frac{a}{I_{ph\text{ref}}} = \frac{aR_{sh}}{(R_s + R_{sh})I_{cc\text{ref}}} \tag{6}
\]

Where \(I_{ph}\) and \(I_0\) are the photovoltaic (PV) and saturation currents, respectively, of the array and \(n_{cs}\) cells connected in series per module. \(R_s\) is the equivalent series resistance of the array and \(R_{sh}\) is the equivalent parallel resistance. Modules connected in parallel increase the current and modules connected in series provide greater output voltages. \(N_s\) and \(N_p\) are the number of modules connected in series and in parallel respectively of the entire array. \(e\) is the electron charge \([1.6 \cdot 10^{-19} \text{C}]\), \(K\) is the Boltzmann constant \([1.38 \cdot 10^{-23} \text{J/K}]\), \(T_c[\text{Kelvin}]\) is the temperature of the p-n junction, and \(A\) is the diode ideality constant.

\[
I_0 = I_{0\text{ref}} \left(\frac{T_c}{T_{cref}}\right)^\frac{3}{2} \exp\left[\frac{E_g}{AK} \left(\frac{1}{T_{cref}} - \frac{1}{T_c}\right)\right] = p_3 T_c^3 \exp\left(-\frac{E_g}{AKT_c}\right) \tag{7}
\]

Where \(E_g\) is the bandgap energy of the semiconductor \((E_g \approx 1.12 \text{eV})\) for the polycrystalline Si at 25\(^\circ\)C and \(T_{cref}\) is the reference temperature.

\[
I_{0\text{ref}} = \frac{I_{cc\text{ref}} \exp\left(\frac{E_g}{AKT_{cref}}\right)}{\exp\left(\frac{E_g}{AK}\right)} \tag{8}
\]

Then \(p_3 = \frac{I_{cc\text{ref}} \exp\left(\frac{E_g}{AKT_{cref}}\right)}{\exp\left(\frac{E_g}{AK}\right)} \left(\frac{T_{cref}}{T_c}\right)^3\) \tag{9}

\[
\Delta T = T_c - T_{cref} \tag{10}
\]

The cell temperature can be determined from ambient temperature and with the help of some standard test information:

\[
T_c = T_a + E \left(\frac{\text{NOCT} - T_{aref}}{800}\right) \tag{11}
\]

### 2.2. Inverter Model

Figure 3 shows a series-connection of single phase inverters. In this asymmetrical multilevel topology, each H-bridge must be fed by an individual DC-voltage and is used to increase the multilevel converter performances, without adding any complexity in the power circuit [8], [9].

![Figure 3. Structure asymmetrical 5, 7 or 9 level cascaded inverter](image)

*Here 7 level \(U_{d1} = 51.9\text{Volt}, U_{d2} = 2U_{d1}*, at standard test conditions (STC)*

Each couple of switches \((K_{dx}, K'_{dx})\), \(x \in \{2j - 1, 2j\}_{j=1-2}\) is controlled by a couple of switching functions \((S_{dx}, S'_{dx})\) such that:

\(A\ Neural\ Network\ Based\ MPPT\ Technique\ Controller\ for\ Photovoltaic\ Pumping\ System\ (Mohammed\ Yaichi)\)
The conversion of the switch commutations in to a voltage is described by a conversion function, $F_{dj}$ such that:

$$F_{dj} = S_d(z_j - 1) - S_d(z_j) \Rightarrow F_{dj} = \{-1, 0, 1\}$$

(13)

The output voltage of each cell is given by:

$$v_{dj} = F_{dj} \cdot U_{dj} = \{-U_{dj}, 0, U_{dj}\}$$

(14)

With $U_{dj}$, the input voltage of each cell.

The output voltage of a phase is given by:

$$v_{so} = F_{d1}U_{d1} + F_{d2}U_{d2}$$

(15)

With: $s, s = a, b$ or $c$; $d, d = 1, 2$ or $3$: represent the number of the phase (leg).

$$E = \begin{bmatrix} v_{an} \\ v_{bn} \\ v_{cn} \end{bmatrix} = \frac{2}{3} \begin{bmatrix} 2 \\ -1 \\ 2 \end{bmatrix} \begin{bmatrix} v_{ao} \\ v_{bo} \\ v_{co} \end{bmatrix}$$

(16)

$E$ is the array input $E = U_{d1} + U_{d2}$.

To improve the output voltage for such inverters, many different modulation strategies have been developed. Among these strategies, the SVM (Space Vector Modulation). This technique provide the nearest switching vectors sequence to the reference vector that is depends the modulation index $r$ without involving trigonometric functions and provide the additional advantages of superior harmonic quality. The generalized algorithm being used to determine, for the hexagonal structure, the exact position of the vector of reference (detection of nearest three vectors and duty cycles computation) was developed and studied in detail in [9].

### 2.3. Motor Asynchronous Model

The mathematical dynamic model of the asynchronous motor is described in [10], [11] by the following equation:

$$\dot{x}(t) = Ax(t) + Bu(t)$$

(17)

With:

$$x^t = \left( l_{ds} l_{qs} \varphi_{dr} \varphi_{qr} \right)^t$$

$$A = \begin{bmatrix} -\lambda & \omega_s & \frac{k_s}{T_r} & \sigma \omega_r & k_s \\ -\omega_s & -\lambda & -\omega_r k_s & \frac{k_s}{T_r} \\ \frac{M}{T_r} & 0 & -\frac{1}{T_r} & \omega_s - \omega_r \\ 0 & \frac{M}{T_r} & -(\omega_s - \omega_r) & -\frac{1}{T_r} \end{bmatrix}$$

$$B = \begin{bmatrix} \frac{1}{\sigma L_s} & 0 & 0 \\ 0 & \frac{1}{\sigma L_s} & 0 \end{bmatrix}$$

$$u = \begin{bmatrix} V_{ds} \\ V_{qs} \end{bmatrix}$$

$$T_r = \frac{l_c}{r_c} ; \sigma = 1 - \frac{M^2}{L_s L_r} ; k_s = \frac{M}{\sigma L_s L_r} ; \lambda = \frac{r_c}{\sigma L_s} + \frac{r_c M^2}{\sigma L_s L_r^2}$$

$d, q$: axes corresponding to the asynchronous reference axes in Park model. $l_{ds}, l_{qs}, \varphi_{dr}, \varphi_{qr}$ are d-axis stator current, rotor flux and q-axis stator current, rotor flux respectively. $L_s, L_r, R_s, R_r$ and $M$ are: stator and rotor main inductances, resistances and mutual inductance respectively. $\sigma$ dispersion factor, $\omega_s$ and $\omega_r$ are the angular speed of the rotating magnetic and electric fields respectively.

The induction motor develops an electromagnetic torque $T_{em}$ expressed as follows:

$$T_{em} = \frac{3}{2} \frac{M}{l_r} (\varphi_{dr} l_{qs} - \varphi_{dr} l_{ds})$$

(18)
$p$ is the number of pole pairs.

### 2.4. Centrifugal Pump Model

The variation of the pump’s speed can give us numerous charts Q-H. The use of a centrifugal pump needs a preliminary study of the most important charts that characterize it, where efficiency will be optimum with the total head and the speed envisaged by control the pumped water quantity to a desirable head. In addition, they are related to dimensions, kinds and speed of the pump.

The chart of the water quantity-head Q-H (Figure 4) explains the different variations in the head of pumping, according to water quantity which forms bent charts. The code then proceeds to the generation of the entire curve. Successively, the program generates a series of characteristics for a fixed range of shaft rotational speeds (generally 35–56 Hz), related to the same pump. It all is done referring to the affinity laws at variable speed. The affinity laws are valid only under conditions of constant efficiency [1], [12]-[13].

\[ Q_{\text{act}} = Q_{\text{des}}(\Omega_{\text{act}}/\Omega_{\text{des}}); \]
\[ HMT_{\text{act}} = HMT_{\text{des}}(\Omega_{\text{act}}/\Omega_{\text{des}})^2; \]
\[ P_{\text{act}} = P_{\text{des}}(\Omega_{\text{act}}/\Omega_{\text{des}})^3 \]
\[ \text{at } \eta_{\text{pace}} = \eta_{\text{pdes}} \]  
\[ (19) \]

Where $Q_{\text{act}}$, $HMT_{\text{act}}$, $P_{\text{act}}$, $\Omega_{\text{act}}$ and $\eta_{\text{pace}}$ are the actual volumetric flowrate, head, the pump shaft input power, rotational speed respectively and the pump efficiency, whereas $Q_{\text{des}}$, $HMT_{\text{des}}$, $P_{\text{des}}$, $\Omega_{\text{des}}$ and $\eta_{\text{pdes}}$ are the same variables referred to the design speed.

Once the characteristic and power demand curves are defined, the pump efficiency may be calculated as follows:

\[ \eta_p = \frac{P_{\text{hyd}}}{k_{ch}H^2} \]  
\[ (20) \]

Where,

\[ P_{\text{hyd}} = CH \cdot Q_{\text{act}} \cdot HMT_{\text{act}} \]  
\[ (21) \]

$P_{\text{hyd}}$ is the power output in terms of pumped water [kW] (i.e. hydraulic output power),

\[ CH = g \cdot \rho = 9.81 \cdot 10^3 \] the constant of gravity,

\[ \rho = 10^3 \cdot k \cdot m^{-3} \] water volumic mass the constant and

\[ k_{ch} \] is the load constant.

![Figure 4. H (Q) Characteristic](image)

Using the relations (19) and the pump datasheet, a set of curves giving the flow versus the head and parameterized by speed can be then obtained, but this procedure is large and in order to use these results during calculations this set of points should be fitted to obtain an algebraic equation, this is done by the use of a two-variables third order polynomial function in order to achieve the best possible regression coefficient [13]:

\[ Q = f(\Omega, HMT) = a + b \cdot \Omega + c \cdot HMT + d \cdot \Omega \cdot HMT + e \cdot \Omega^2 + f \cdot HMT^2 + g \cdot \Omega^2 \cdot HMT + h \cdot \Omega^3 + i \cdot HMT^3 + j \cdot \Omega \cdot HMT^2 + k \cdot \Omega^2 \cdot HMT \]  
\[ (22) \]
For the determination of the pump operating point it is required to know both the pump and pipeline characteristics. The piping system deals with the total head that must be overcome by the pump. The Q-H characteristic of the pipe network is given as a function of the geodetic head and head losses (as function of the flow-rate) \cite{14}. Thus, it should at least equal the head corresponding the flow computed by the pump flow-head equation. It comes:

\[ HMT = H_g + kQ^2 \]  

(23)

The constant \( k \) relates to the head loss caused by fluid friction. \( H_g \): Geodetic head.

2.5. Vectorial Command Approach

The vector control is based on the field-oriented control (FOC) method. For the regulation of the main variables (current, flux, speed) to their reference values, regulators were used of the type PI \cite{10}, \cite{11}. So we have as interest to keep only the \( d \) axis flux component, and that means to oblige the \( q \) axis flux component to be zero.

\[ \varphi_{ar} = 0 \quad \text{and} \quad \varphi_{dr} = \varphi_r \]  

(24)

The flux and torque will be reduced respectively then to:

\[ \varphi_r = \frac{M}{1 + j\tau_r} I_{ds} \]  

(25)

\[ T_{em} = \frac{3}{2} P M \frac{1}{\tau_r} \varphi_{dr} I_{qs} \]  

(26)

Therefore the \( d \) and \( q \) axis statoric voltages equations will be:

\[
\begin{align*}
V_{ds} &= \lambda \sigma L_s I_{ds} + \sigma L_s \frac{dI_{ds}}{dt} - \sigma L_s \omega_s I_{qs} - \frac{k_s}{\tau_r} \lambda L_s \varphi_r \\
V_{qs} &= \lambda \sigma L_s I_{qs} + \sigma L_s \frac{dI_{qs}}{dt} + \sigma L_s \omega_s I_{ds} + \sigma L_s \omega_s \varphi_r \\
\omega_{qs} &= \omega_s - \omega = \frac{M}{\varphi_r \tau_r} I_{qs}
\end{align*}
\]  

(27)

The compensation has as objective to uncouple the two \( d \) and \( q \) axis voltages and currents. Under such conditions, the system becomes linear like in case of DC motor. Thus we have:

\[
\begin{align*}
V_{ds} &= V_{ds1} - fem_d \\
V_{qs} &= V_{qs1} + fem_q
\end{align*}
\]  

(28)

Where,

\[ fem_d = \sigma L_s \omega_s I_{qs} + \frac{k_s}{\tau_r} \lambda L_s \varphi_r \]  

(29)

\[ fem_q = \sigma L_s \omega_s I_{ds} + \sigma L_s \omega_s \varphi_r - \sigma L_s k_s \frac{M}{\tau_r} I_{qs} \]  

(30)

Are the compensation voltages.

The transfer functions of the plant for the controllers of the vector-controlled induction motor drives can be derived as shown in \cite{10}, \cite{11}.

Speed, \( I_{ds} \) and \( I_{qs} \) current controllers:

\[
\begin{align*}
G_{io} &= \frac{a_i}{i_{em}} = \frac{p}{f_c + js} \\
G_{I_{ds}} &= \frac{i_{ds}}{V_{ds}} = \frac{1}{\lambda \sigma L_s + \sigma L_s} \\
G_{I_{qs}} &= \frac{i_{qs}}{V_{qs}} = \frac{1}{\lambda \sigma L_s + \sigma L_s}
\end{align*}
\]  

(31)

Where \( s \) is the Laplace operator.
Based on those equations and after some algebra (Imposition of the poles method) we obtain PI parameters for speed and current (Table 1), were \( J \) is the rotor inertia moment, \( f_\epsilon \) is the viscosity coefficient of the induction motor. After \( \delta \) is obtained upon calculation of the transfer function of a closed loop, parameters \( K_p \) and \( K_i \) are identified from imposition of the poles method. A wise choice the \( K_p \) and \( K_i \) was made by changing the value of \( \delta \).

### Table 1. PI Regulator Coefficients

<table>
<thead>
<tr>
<th>Coefficients</th>
<th>( k_p )</th>
<th>( k_i )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Current</td>
<td>( \frac{2E_R R_N K_T}{\omega_i I_i^2} )</td>
<td>( \frac{2E_R^2}{I_i} )</td>
</tr>
<tr>
<td>Speed ( \omega )</td>
<td>( \frac{2E_R f_\epsilon}{I_i} )</td>
<td>( \frac{2E_R^2}{f_\epsilon} )</td>
</tr>
</tbody>
</table>

3. **LOCATION OF MAXIMUM POWER POINT**

At the maximum power point we have:

\[
\frac{d(V_{pp}\cdot i_{pp})}{di_{pp}} = 0 \Rightarrow V_{pp} + I_{pv} \frac{dV_{pp}}{di_{pp}} = 0 \tag{32}
\]

With the current described by equation (01), the voltage may be expressed as:

\[
V_{pp} = -\left( \frac{N_s R_s}{N_p} \right) I_{pv} + \frac{A N_c_2 N_p K_T e_0}{e_0} \log \left[ \frac{I_{pv} - N_p R_p E (1 + p_2 \Delta T) + N_p}{N_p R_s} \right] \tag{33}
\]

Back substitution of the partial derivative of \( V_{pp} \) with respect to \( I_{pv} \) and using \( V_{pv,op} \) for \( V_{pp} \) and \( I_{pv,op} \) for \( I_{pv} \) gives:

\[
\log \left[ \frac{I_{pv,op} - N_p R_p E (1 + p_2 \Delta T) + N_p}{N_p R_s} \right] + 1 \left( \frac{1 + \frac{R_s}{R_p}}{I_{pv,op} - N_p R_p E (1 + p_2 \Delta T) + N_p e_0 \frac{R_s}{R_p} + N_p R_s e_0 \frac{R_s}{R_p} - N_p R_s e_0 \frac{R_s}{R_p} \exp \left( -\frac{E_R}{A N_c_2 N_p K_T} \right) - \frac{2R_s e_0}{N_p A N_c_2 N_p K_T} \right) I_{pv,op} = 0 \tag{34}
\]

With \( V_{pv,op} \) and \( I_{pv,op} \) the voltage and current at maximum power.

Numerical method is applied to solve for \( I_{pv,op} \) using an initial guess given by:

\[
I_{pv,op,guess} \leq N_p R_p E (1 + p_2 \Delta T) \quad \text{or} \quad I_{pv,op,guess} = N_p \frac{E}{E_{ref}} (I_{pv,op,ref} + a \Delta T) \tag{35}
\]

We obtain a relation linear which can be expressed by:

\[
I_{pv,op} = 0.9325 N_p I_{ph} + 0.0142 \tag{36}
\]

Once \( I_{pv,op} \) is found, \( V_{pv,op} \) may be calculated using equation (33) and thus the current and voltage at the maximum power point is determined as a consequence the maximum power.

\[
P_{pv,max} = V_{pv,op} I_{pv,op} - N_s N_p R_s \left( 0.94 p_1 E (1 + p_2 \Delta T) \right)^2 + \frac{0.94 N_p R_p E (1 + p_2 \Delta T) A N_c_2 N_p K_T e_0}{e_0} \log \left[ \frac{0.94 R_s}{R_p} - 0.06 N_p R_p E (1 + p_2 \Delta T) \exp \left( -\frac{E_R}{A N_c_2 N_p K_T} \right) + 1 \right] \tag{37}
\]

At optimal regime, for calculation the speed reference, the assessment of power of asynchronous motor is given by:

\[
A Neural Network Based MPPT Technique Controller for Photovoltaic Pumping System (Mohammed Yaichi)\]
The relations governing the operation of the motor-pump [15].

\[ P_{pv,max} - 3R_{sm}I_{s,rms}^2 = P_{pv,max} - \frac{3}{2}R_{sm}I_s^2 = P_t \]  
(38)

By substituting equations \( I_{qs} \) and \( \omega_{gl} \) into Equation (41).

\[ I_{qs} = \frac{2k_{ch}}{3p^3M^2} \cdot \omega^2 \]  
(43)

\[ \omega_{gl} = \frac{2Rr_k}{3p^3M^2} \cdot \omega^2 \]  
(44)

By rearranging the Equation (45) gives:

\[ a\omega^4 + b\omega^3 + c = 0 \]  
(47)

4. NEURAL NETWORK BASED MPPT

The ANN theory, in general, has been well-discussed in the literature [16]-[18], and a number of authors [3], [4], [19] have described its operation in the PV system and for speed control of an induction motor. Neural network architecture is specified through finding the appropriate solution for the non-linear and complex systems or the random variable ones. Among its types, the more widespread, important and useful back propagation network. The function and results of an artificial neural network are determined by its architecture that has different kinds. The simpler architecture contains three layers as shown in Figure 6. The input layer receives the extern data. The second layer, hidden layer, contains several hidden neurons which receive data from the input layer and send them to the third layer, output layer. This later responds to the system.
We can conclude unlimited neural network architectures. The more several hidden layers and neurons in each layer are added; the more complex they become. The network is fully connected which a bias signal is coupled to all neurons in the hidden layer through a weight \( W \). The realization of the back propagation network is based on two main points: learning and knowledge. This research was applied by the use of sigmoid function as an activation function in order to calculate the hidden layer output and the linear function to calculate the output.

In our study of the effect of network architecture on learning, we have chosen architecture with one hidden layer. We have changed the number of neurons in hidden layer; this architecture is summarized in Table 2. By 5 neurons in hidden layer, the regression coefficient R-square \( (R^2) \) increases to 0.9999.

<table>
<thead>
<tr>
<th>Number of neurons in hidden layer</th>
<th>( R^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>0.9984</td>
</tr>
<tr>
<td>5</td>
<td>0.9999</td>
</tr>
<tr>
<td>8</td>
<td>0.9991</td>
</tr>
<tr>
<td>9</td>
<td>0.9989</td>
</tr>
<tr>
<td>11</td>
<td>0.9991</td>
</tr>
</tbody>
</table>

Figure 5 shows the proposed ANN topology, it use multilayer perceptron type network consists of an input layer, one hidden layer and an output layer with sigmoidal type transfer function. The composite network uses two neurons at the input, one for the radiation and the other for the ambient temperature, which is normalized and then pulse neurons in the hidden layer. The output layer has only one neuron for the control DC/AC frequency.

The procedure described in the previous section will be utilized to generate training data for ANN-based MPPT.

The outputs are calculated by the following equation:

\[
a_i^{(2)}(t) = \sum_{j=1}^{2} W_{ij}^{(2)} \cdot X_j^{(1)} \quad \text{with:} \quad i = 1 \ldots 5
\]

\[
X_i^{(2)}(t) = f[a_i^{(2)}(t)]
\]

\[
y^{(3)}(t) = \sum_{j=1}^{5} W_j^{(3)} \cdot X_j^{(2)}
\]

The update of \( W \) is done according to the rule of delta:

\[
A Neural Network Based MPPT Technique Controller for Photovoltaic Pumping System (Mohammed Yaichi)
\[ W_{ji}^{(2)} = W_{ji}^{(2)} + \Delta W_{ji} \quad \text{and} \quad W_{j}^{(3)} = W_{j}^{(3)} + \Delta W_{j} \]

(51)

Where: \( J = \frac{1}{2} (y_{\text{desired}} - y^{(3)})^2 \), \( \Delta W_{ji} = \alpha \frac{\partial J}{\partial W_{ji}} \) and \( \Delta W_{j} = \alpha \frac{\partial J}{\partial W_{j}} \)

(52)

With \( \alpha \) is the step of training and,

\[ \frac{\partial J}{\partial W_{ji}} = \delta_{\text{output}} \cdot X_j^{(2)} \] \( , \delta_{\text{output}} = -(y_{\text{desired}} - y^{(3)}) \)

(53)

\[ \frac{\partial J}{\partial W_{ji}} = \delta_{\text{hidden}} \cdot X_j^{(3)} \] \( , \delta_{\text{hidden}} = -(y_{\text{desired}} - y^{(3)}) \cdot W_i^{(3)} \cdot f'[a_i^{(2)}(t)] \)

(54)

Algorithm architecture of the back propagation implies the following steps as shown in Figure 6.

The results of ANN-based MPPT at five operating case (proposed learning examples) were found that the output speed response of the motor-pump with analytical results is higher than the inputs radiation and ambient temperature as shown in Figure 7 (a)-(e) which shows the output of ANN at five case and shows the corresponding data with the analytical results. Also, the MPPT method was validated for the case 37°C and compared with the data, they were found to correlate very well (Test of generalization in Figure 8). This means that the network can be operated at any conditions climatic.
A Neural Network Based MPPT Technique Controller for Photovoltaic Pumping System (Mohammed Yaichi)
5. RESULTS AND DISCUSSION

The Model field-oriented control using MPPT technique is developed and studied in detail in another work [1].

![Block diagram of a field-oriented control induction motor coupled to a centrifugal pump, fed by solar cells through an inverter](image)

Figure 9. The block diagram of a field-oriented control induction motor coupled to a centrifugal pump, fed by solar cells through an inverter

![Graphs showing radiation, PV array voltage, reference speed, frequency, flux, electromagnetic torque, flow rate, and pump efficiency](image)

Figure 10. Behavior of the pump by considering radiation variations

Figure 9 gives a diagrammatic sight of a drive at variable speed using the principle of the field-oriented control. For the simulation results used in this paper, the numerical values for the PV array and the pump SP5A7 are summarized in Table 3-4. The numerical values of the simulation model are obtained either by measurements or identification from laboratory experiments.

In order to verify the proposed model, digital simulations were carried out for four insulation level. At the beginning, radiation is worth $G=540\,\text{W/m}^2$, then radiation is brought to $G=1200\,\text{W/m}^2$ in 1s then in $G=940\,\text{W/m}^2$ in 3s and finally, radiation reached $G=150\,\text{W/m}^2$ in 6s.
A Neural Network Based MPPT Technique Controller for Photovoltaic Pumping System (Mohammed Yaichi)

Table 3. PV array specifications [7]

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Isotón Array; Dimensions: (1.224 × 0.545)m²</td>
<td>Weight = 9 kg, Panel Efficiency: η = 11.2%, Fill Factor FF = 74.4%</td>
</tr>
<tr>
<td>Cell type</td>
<td>Monocrystalline cell</td>
</tr>
<tr>
<td>Peak power $P_{	ext{max}}$ [W]</td>
<td>75 ± 10%</td>
</tr>
<tr>
<td>Optimal voltage $V_{	ext{opt}}$ [Volt]</td>
<td>17.3</td>
</tr>
<tr>
<td>Optimal current $I_{	ext{opt}}$ [A]</td>
<td>4.34</td>
</tr>
<tr>
<td>Open circuit Voltage $V_{oc}$ [Volt]</td>
<td>21.6</td>
</tr>
<tr>
<td>Short Circuit current $I_{sc}$ [A]</td>
<td>4.67</td>
</tr>
<tr>
<td>Cell number $n_c$</td>
<td>36</td>
</tr>
<tr>
<td>Temperature Coefficient of $I_{sc}$ $a$ [%/°C]</td>
<td>0.02</td>
</tr>
<tr>
<td>Reference ambient temperature $T_{amb}$ [°C]</td>
<td>20</td>
</tr>
<tr>
<td>Diode ideality constant $A$</td>
<td>1.2</td>
</tr>
<tr>
<td>Photo current $I_{ph}$ [A]</td>
<td>4.6756</td>
</tr>
<tr>
<td>Equivalent series resistance of the panel $R_s$ [Ω]</td>
<td>0.2402</td>
</tr>
<tr>
<td>Equivalent parallel resistance $R_{in}$ [Ω]</td>
<td>199.4843</td>
</tr>
<tr>
<td>$p_1$</td>
<td>0.0047</td>
</tr>
<tr>
<td>$p_2$</td>
<td>1.9976 × 10⁻⁴</td>
</tr>
<tr>
<td>$p_3$</td>
<td>3.7042</td>
</tr>
<tr>
<td>PV array: Number of modules connected in series and in parallel</td>
<td>9 Ns × 1 Np</td>
</tr>
</tbody>
</table>

Table 4. Motor-pump specifications [1, 20]

<table>
<thead>
<tr>
<th>Subsystem</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pump</td>
<td>Load Constante $k_{m}$ [N · m · (s/ rad)]²</td>
</tr>
<tr>
<td>Type</td>
<td>Grunfos Ms 402</td>
</tr>
<tr>
<td>RMS motor voltage $V$ [ Volt]</td>
<td>65Δ</td>
</tr>
<tr>
<td>Maximal current $I$ [A]</td>
<td>8.5</td>
</tr>
<tr>
<td>Speed $\Omega$ [r/min]</td>
<td>2860</td>
</tr>
<tr>
<td>Power $P$ [kW]</td>
<td>0.55</td>
</tr>
<tr>
<td>Motor frequency freq [Hz]</td>
<td>50</td>
</tr>
<tr>
<td>Stator resistance per phase $R_{eq}$ [Ω]</td>
<td>0.6667</td>
</tr>
<tr>
<td>Motor power factor cos(ω)</td>
<td>0.8</td>
</tr>
<tr>
<td>Rotor resistance $R_{s}$ [Ω]</td>
<td>1.965</td>
</tr>
<tr>
<td>Rotor leakage inductance $L_{r}$ [H]</td>
<td>0.0895</td>
</tr>
<tr>
<td>Rotor inductance $L_{m}$ [H]</td>
<td>0.087</td>
</tr>
<tr>
<td>Mutual inductance $M$ [H]</td>
<td>0.087</td>
</tr>
<tr>
<td>Pair pole number $p$</td>
<td>1</td>
</tr>
<tr>
<td>Inertie Torque $[\text{kg}·\text{m}^2]$</td>
<td>0.003</td>
</tr>
<tr>
<td>Friction coefficient $f_r$ $[\text{N}·\text{m}·\text{s}/\text{rad}]$</td>
<td>2.905 × 10⁻⁴</td>
</tr>
<tr>
<td>Efficiency η [%]</td>
<td>0.78</td>
</tr>
<tr>
<td>Flux $Q$ [Wb]</td>
<td>0.28 – 0.3</td>
</tr>
</tbody>
</table>

The response of the system using MPPT controller obtained by simulation is shown in Figure 10. All test results show that the robust tracking speed of induction motor drive with the proposed MPPT control strategy is very effective in tracking the selected tracks at all times, it is observed that, in every case. This controller provides a very useful tool for ensuring optimal efficiency, which essentially keeps its state optimal. On the other hand, the results show the output voltage responses of the PV array to the change of radiation and temperature. For example, at 3s the radiation stepping stepping-down from 1200 to 940 W/m², the PV array voltage stepping-up from 118 to 122 volt. This system is able to adapt the operating point according to variations of the radiation and the temperature (random variation).

The PI controller brings the measured speed to the desired value smoothly and without the overshoot. We observed the flow estimation and also the resistive torque imposed by the quantity of pumped water. The electromagnetic torque compensates for instantaneously this request of the resistive torque. The figures show that the flow and the couple are decoupled. In addition, flow is constant in permanent mode $\varphi_1 = 0.28 \text{wb}$. The statoric voltage by frequency ratio is always kept constant with a $V/\Omega$ value of 1.3 during operation, the motor is thus, managed by the $V/\Omega$ constant law, which shows the effectiveness of the loop of speed regulation.

6. CONCLUSION

An optimal operation of a photovoltaic pumping system based on an induction motor was described. A neural network based MPPT has been investigated that operates very well in the PV pumping system. The proposed structure allows at the same time the field oriented control and the maximum power tracking of the photovoltaic array.
This control has given very good results; where it assured a total decoupling between the system parameters. Moreover, it assured a good tracking of the speed with a minimum response time. The regression coefficient R-square ($R^2$) arises in high values through the neural network with one hidden layer, with 5 neurons. The proposed algorithm in neural networks was simulated; the simulation results show that this system is able to adapt the maximum operating point according to variations in external disturbances. In addition, the proposed approach does not need two converters; it uses only a DC/DC converter. Also, increase of both the daily pumped quantity and array PV efficiency are reached by the proposed approach.

REFERENCES
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